

104 - EQ - 6.1 Rational Expressions 2

Use the following information to answer Q1:

A student is working on a Rational Expressions question. Their work is shown below.

Line 1	$\frac{x^2+2x-15}{x^2+11x+30}$	
Line 2	$\frac{(x+5)(x-3)}{(x+5)(x+6)}$	↙
Line 3	$\frac{(x-3)}{(x+6)}$, where $x \neq -6$	$\frac{(x-3)}{(x+6)}$, where $x \neq -5, -6$

Q1: What mistake did the student make?

- The student factored the numerator incorrectly.
- The student factored the denominator incorrectly.
- The student simplified the expression incorrectly.
- The student incorrectly stated the Non-Permissible Value(s).

Q2: (Long Answer) Determine the height of the rectangle, and state any non-permissible values. (2 marks)

Area
 $3x^2 - 4x - 4$

← $3x^2 - 3x - 6$ →

Area = L × H

$$H = \frac{\text{Area}}{\text{Length}} = \frac{(3x^2 - 4x - 4)}{(3x^2 - 3x - 6)}$$

$3x^2 - 4x - 4$	$\begin{matrix} +2 & -6 \\ \square + \square = -4 \\ \square \times \square = -12 \end{matrix}$	$3x^2 - 3x - 6$
↓		
$3x^2 + 2x - 6x - 4$		$3(x^2 - x - 2)$
$(3x^2 + 2x) + (-6x - 4)$		$\begin{matrix} +1 & -2 \\ \square + \square = -1 \\ \square \times \square = -2 \end{matrix}$
$x(3x+2) - 2(3x+2)$		$3(x+1)(x-2)$
$(3x+2)(x-2)$		

MARKING:

Beginning	0.0 - 1.0
Progressing	1.5 - 2.0
Competent	2.5
Exemplary	3.0

$$H = \frac{(3x^2 - 4x - 4)}{(3x^2 - 3x - 6)} = \frac{(3x+2)(x-2)}{3(x+1)(x-2)}$$

$$H = \frac{3x+2}{3(x+1)}, \text{ where } x \neq -1, 2$$