

104 - Worksheet - 6.2 Multiplying and Dividing Rational Expressions

Pg 327 #8abc: Express each quotient in simplest form. Identify all non-permissible values.

$$\frac{2w^2 - w - 6}{3w + 6} \div \frac{2w + 3}{w + 2}$$

$w \neq -3/2$

$$\frac{(2w+3)(w-2)}{3(w+2)} \div \frac{(2w+3)}{(w+2)}$$

$w \neq -2$        $w \neq -2$

$$\frac{(2w+3)(w-2)}{3(w+2)} \cdot \frac{(w+2)}{(2w+3)}$$

$$\frac{(w-2)}{3}$$

where  $w \neq -2, -3/2$

$$\frac{v-5}{v} \div \frac{v^2-2v-15}{v^3}$$

$v \neq -3$      $v \neq 5$

$$\frac{(v-5)}{v} \div \frac{(v+3)(v-5)}{v^3}$$

$v \rightarrow v \neq 0$        $v^3 \rightarrow v \neq 0$

$$\frac{(v-5)}{v} \cdot \frac{v^3}{(v+3)(v-5)}$$

$$\frac{v^3}{v(v+3)}$$

$$\frac{v^2}{(v+3)}$$

where  $v \neq -3, 0, 5$

$$\frac{9x^2-1}{x+5} \div \frac{3x^2-5x-2}{2-x}$$

$x \neq -1/3$      $x \neq 2$

$$\frac{(3x+1)(3x-1)}{(x+5)} \div \frac{(3x+1)(x-2)}{-1(x-2)}$$

$x \neq -5$        $x \neq 2$

$$\frac{(3x+1)(3x-1)}{(x+5)} \cdot \frac{(-1)(x-2)}{(3x+1)(x-2)}$$

$$\frac{-1(3x-1)}{(x+5)}$$

where  $x \neq -5, -1/3, 2$

Pg 327 #9: Explain why the non-permissible values in the quotient  $\frac{x-5}{x+3} \div \frac{x+1}{x-2}$  are -3, -1, 2.

Can't divide by zero, so numerator can't be zero.  $x \neq -1$ .

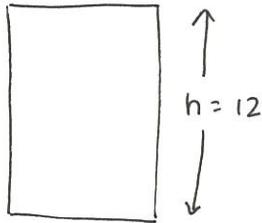
$\frac{x-5}{x+3}$      $\frac{x+1}{x-2}$

This number can't be undefined.  $x \neq -3$

This number can't be undefined.  $x \neq 2$

**Pg 327 #10:** The height of a stack of plywood is represented by  $\frac{n^2-4}{n+1}$ . If the number of sheets is defined by  $n - 2$ , what expression could be used to represent the thickness of one sheet? Express your answer in simplest form.

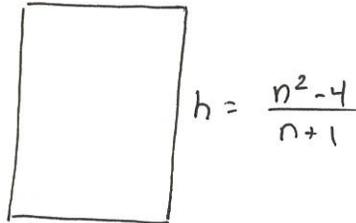
EASY EXAMPLE



If there are 6 sheets, what is the thickness of each sheet?

Thickness =  $12 \div 6$

OUR EXAMPLE



There are  $n-2$  sheets

Thickness =  $\frac{n^2-4}{n+1} \div n-2$

$$\frac{(n+2)(n-2)}{(n+1)} \div \frac{(n-2)}{1}$$

$n \neq 2$

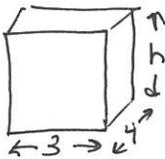
$$\frac{(n+2)(\cancel{n-2})}{(n+1)} \cdot \frac{1}{(\cancel{n-2})}$$

$\hookrightarrow n \neq -1$

Thickness =  $\frac{(n+2)}{(n+1)}$   
 where  $n \neq -1, 2$

**Pg 328 #11c:** Simone is shipping his carving to a buyer in Winnipeg. He makes a rectangular box with a length of  $(2x - 3)$  meters and width of  $(x + 1)$  meters. The volume of the box is  $(x^2 + 2x + 1)$  cubic meters. What is an expression for the height of the box?

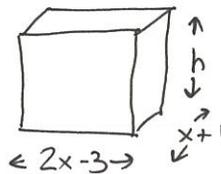
EASY EXAMPLE



VOL = 24

$h = \frac{VOL}{(4)(3)}$

OUR EXAMPLE



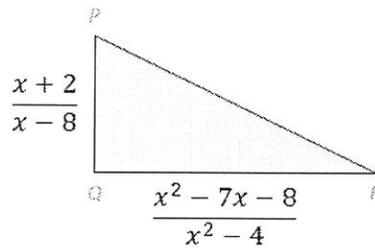
VOL =  $(x^2 + 2x + 1)$

$h = \frac{(x^2 + 2x + 1)}{(2x-3)(x+1)}$

=  $\frac{(x+1)(x+1)}{(2x-3)(x+1)}$   $x \neq -1, -1$   
 $x \neq -1, 3/2$

=  $\frac{(x+1)}{(2x-3)}$  where  $x \neq -1, 3/2$

**Pg 328 #16:** What is an expression for the area of  $\triangle PQR$ ? Give your answer in simplest form.



$$\begin{aligned}
 \text{Area} &= \frac{1}{2} (b)(h) \\
 &= \frac{1}{2} \cdot \frac{(x+2)}{(x-8)} \cdot \frac{(x^2 - 7x - 8)}{(x^2 - 4)} \\
 &= \frac{1}{2} \cdot \frac{\cancel{(x+2)}}{\cancel{(x-8)}} \cdot \frac{\cancel{(x-8)}(x+1)}{(x+2)(x-2)} \\
 &\quad \downarrow \quad \quad \quad \downarrow \quad \downarrow \\
 &\quad x \neq 8 \quad \quad \quad x \neq -2 \quad x \neq 2 \\
 &= \frac{(x+1)}{2(x-2)} \quad \text{where } x \neq -2, 2, 8
 \end{aligned}$$

**Pg 329 #18:** The volume,  $V$ , of a gas increases or decreases with its temperature,  $T$ , according to Charles' law by the formula  $\frac{V_1}{V_2} = \frac{T_1}{T_2}$ . Determine  $V_1$  if  $V_2 = \frac{n^2 - 16}{n - 1}$ ,  $T_1 = \frac{n - 1}{3}$ , and  $T_2 = \frac{n + 4}{6}$ . Express your answer in simplest form.

$$\frac{V_1}{V_2} = \frac{T_1}{T_2} \Rightarrow V_1 = \frac{T_1 V_2}{T_2} \Rightarrow V_1 = T_1 \cdot V_2 \div T_2$$

$$V_1 = \frac{(n-1)}{3} \cdot \frac{(n^2-16)}{(n-1)} \div \frac{(n+4)}{6}$$

$$V_1 = \frac{(n-1)}{3} \cdot \frac{(n+4)(n-4)}{(n-1)} \div \frac{(n+4)}{6} \quad \rightarrow n \neq -4$$

$$\quad \quad \quad \downarrow$$

$$\quad \quad \quad n \neq 1$$

$$V_1 = \frac{\cancel{(n-1)}}{3} \cdot \frac{\cancel{(n+4)}(n-4)}{\cancel{(n-1)}} \cdot \frac{6}{\cancel{(n+4)}}$$

$$V_1 = 2(n-4) \quad \text{where } n \neq -4, 1$$