

First Name: _____

Last Name: _____

L18 - EQ - 4.2 factoring Quadratic Equations

Q1: The roots of the equation $2x^2 = 4x + 6$ are $x = a, -b$, where a and b are ____ and ____.

Reminder: The "roots" of the quadratic are the numbers that satisfy the quadratic equation.

(Record your answer in the Numerical Response boxes below)

3	1		
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$$\begin{aligned}
 2x^2 &= 4x + 6 \\
 -4x \quad -4x \\
 2x^2 - 4x &= 6 \\
 -6 \quad -6 \\
 2x^2 - 4x - 6 &= 0 \\
 2(x^2 - 2x - 3) &= 0 \\
 2(x - 3)(x + 1) &= 0 \\
 \downarrow \qquad \qquad \downarrow \\
 x - 3 = 0 & \qquad \qquad x + 1 = 0 \\
 \boxed{x = 3} & \qquad \qquad \boxed{x = -1}
 \end{aligned}$$

Q2: Factor the expression. (2 marks)

$$\begin{aligned}
 (x-5)^2 + 8(x+5) + 12 & \qquad \text{Let } y = x-5 \\
 y^2 + 8y + 12 & \\
 \boxed{(y + 2)(y + 6)} & \text{ 1 mark} \\
 (x-5 + 2)(x-5 + 6) & \\
 \boxed{(x - 3)(x + 1)} & \text{ 1 mark}
 \end{aligned}$$

KEY

Q3: Solve the Rational Equation (this will not be on your Chapter 4 SQ, but will be on the Unit Test... don't forget to keep reviewing it).

(2 marks)

$$\frac{x+3}{x+5} + \frac{x+4}{x+6} = \frac{5}{6}$$

1/2 mark

$$\frac{x+3}{x+5} \left(\frac{x+6}{x+6} \right) \left(\frac{6}{6} \right) + \frac{x+4}{x+6} \left(\frac{x+5}{x+5} \right) \left(\frac{6}{6} \right) = \frac{5}{6} \left(\frac{x+5}{x+5} \right) \left(\frac{x+6}{x+6} \right)$$

$$x \neq -6, -5$$

$$\frac{(x^2+9x+18)6}{(x+5)(x+6)(6)} + \frac{(x^2+9x+20)(6)}{(x+6)(x+5)(6)} = \frac{5(x^2+11x+30)}{6(x+5)(x+6)}$$

Looking at numerator...

$$(6x^2 + 54x + 108) + (6x^2 + 54x + 120) = (5x^2 + 55x + 150)$$

$$\begin{array}{r} 12x^2 + 108x + 228 = 5x^2 + 55x + 150 \\ -5x^2 \qquad \qquad \qquad -5x^2 \end{array}$$

$$\begin{array}{r} 7x^2 + 108x + 228 = 55x + 150 \\ -55x \qquad \qquad \qquad -55x \end{array}$$

$$\begin{array}{r} 7x^2 + 53x + 228 = 150 \\ -150 \qquad -150 \end{array}$$

1/2 mark $7x^2 + 53x + 78 = 0$

$$7x^2 + 14x + 39x + 78 = 0$$

$$(7x^2 + 14x) + (39x + 78) = 0$$

$$7x(x+2) + 39(x+2) = 0$$

$$(x+2)(7x+39) = 0$$

1/2 mark $x = -2$

1/2 mark $x = -\frac{39}{7}$

$$\begin{array}{l} 14 \quad +39 \\ \square + \square = 53 \\ \square \times \square = 546 \end{array}$$

- 1, 546
- 2, 273
- 3, 182
- 6, 91
- 7, 78
- 13, 42
- 14, 39

MARKING:

Beginning	0-2.0
Progressing	2.5-3.5
Competent	4.0-4.5
Exemplary	5.0