

1.29 - 6.4 Function Notation

GIVEN $f(x)=2x-2$, FIND $f(-5)$:

$$f(x) = 2x - 2$$

$$f(-5) = 2(-5) - 2$$

$$f(-5) = -10 - 2$$

$$f(-5) = -12$$

Part 1 - What is a Function?

A function is a relation in which each value of the independent variable is associated with exactly one value of the dependent variable.

“Each value of x has only one value for y ”

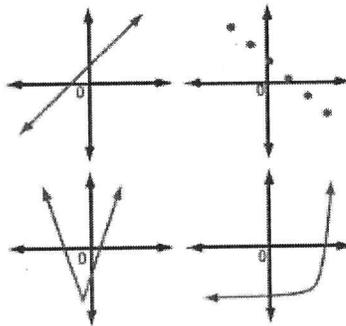
Functions:

These 8 relations are functions.

x	y	x	y
5	10	11	3
6	15	21	3
7	20	31	3

$\{(-2, -5), (0, 4), (2, 13), (4, 22)\}$

$\{(10, 10), (12, 10), (14, 12), (16, 12)\}$



For any x -value, only one y -value.

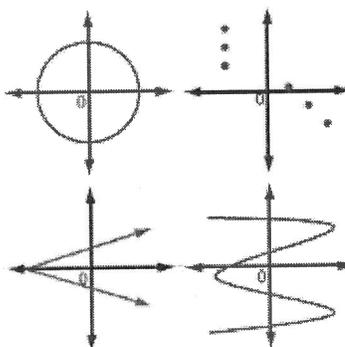
Not Functions:

These 8 relations are not functions.

x	y	x	y
6	10	3	11
6	15	3	21
7	20	3	31

$\{(10, 10), (12, 10), (12, 14), (12, 16)\}$

$\{(7, 5), (7, 8), (9, 11), (11, 14)\}$



Some x -values have multiple y -values.

All fail “vertical line test” described below.

Both **Functions** and **Non-Functions** are still **relations**, and relate x -values to y -values.

Vertical Line Test – If any vertical line intersects the graph at more than one point, the relation is not a function.

Math 10C

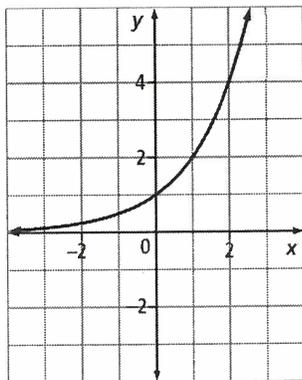
Determine whether each relation is a function or is not a function. Give reasons for your answer.

(4, 1), (5, -2), (6, -5), (7, -8), (6, -11), (5, -14), (4, -17)

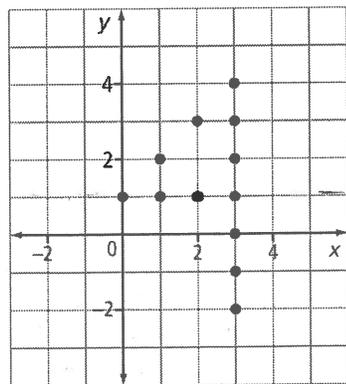
When $x=5$, $y=-2$ and -14 .
Not a function.

x	y
-2	-2
-1	4
0	-8
1	16
2	-32

Every x only has one y -value.
Function!



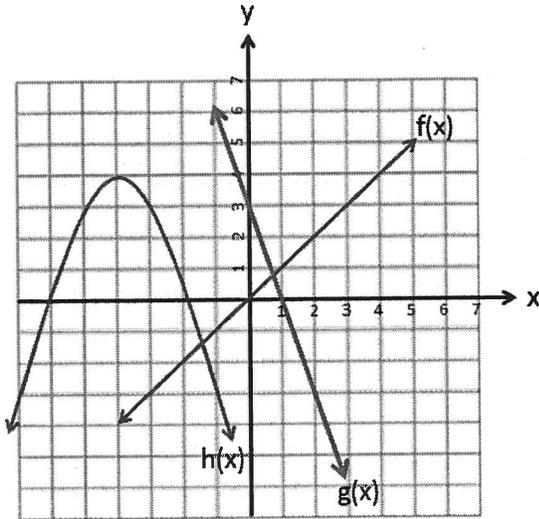
Every x only has one y -value.
Function!



When $x=3$, multiple y -values.
Fails vertical line test.
Not a function.

Part 2 – What is Function Notation?

Use the following graph to answer the next few questions:



Q1: What is y when $x=-3$ for the red graph?

Q2: What is y when $x=-1$ for the blue graph?

What is the problem with asking questions this way?

*All the graphs are grey on my handout!
Why can't we just refer to them by the "f(x)" labels?*

Use the following equations to answer the next few questions:

$$y = x$$

$$y = -3x + 3$$

$$y = -\frac{7}{9}x^2 - \frac{56}{9}x - \frac{76}{9}$$

Uh... still grey. Might look good on the Smart Notebook lesson, but I can't tell the difference.

Q3: What is y when $x=-3$ for the red equation?

Q4: What is y when $x=-1$ for the blue equation?

What is the problem with asking questions this way?

*Printer prints in Black + white.
I would prefer to use the "f(x)" labels.*

Part 3 – Function Notation – Solving for “y”

Functions can be written in a different notation where y is replaced with f(x):

$$y = 4x + 1$$

$$f(x) = 4x + 1$$

Use the following equations to answer the next few questions:

$$f(x) = x$$

$$g(x) = -3x + 3$$

$$h(x) = -\frac{7}{9}x^2 - \frac{56}{9}x - \frac{76}{9}$$

Q5: What is f(-3) = ?

or what is y when x = -3 for the “f(x)” equation?

$$f(x) = x$$

$$f(-3) = -3$$

so when x = -3, y = -3. \Rightarrow Point (-3, -3) on graph.

Q6: What is h(-1) = ?

or what is y when x = -1 for the “h(x)” equation?

$$h(-1) = -\frac{7}{9}(-1)^2 - \frac{56}{9}(-1) - \frac{76}{9}$$

$$= -\frac{7}{9} + \frac{56}{9} - \frac{76}{9}$$

$$= -\frac{27}{9}$$

$$= -3$$

so when x = -1, y = -3 \Rightarrow Point (-1, -3) on graph.

Q7: What is g(4) = ?

or what is y when x = 4 for the “g(x)” equation?

$$g(4) = -3(4) + 3$$

$$= -12 + 3$$

$$= -9$$

so when x = 4, y = -9 \Rightarrow Point (4, -9) on graph.

Q8: What is h(-4) = ?

or what is y when x = -4 for the “h(x)” equation?

$$h(-4) = -\frac{7}{9}(-4)^2 - \frac{56}{9}(-4) - \frac{76}{9}$$

$$= -\frac{7}{9}(16) - \frac{56}{9}(-4) - \frac{76}{9}$$

$$= -\frac{112}{9} + \frac{224}{9} - \frac{76}{9}$$

$$= \frac{36}{9}$$

$$= 4$$

so when x = -4, y = +4 \Rightarrow Point (-4, 4) on graph.

Part 4 – Function Notation – Solving for “x”

Use the following equations to answer the next few questions:

$f(x) = x$

$g(x) = -3x + 3$

$h(x) = -\frac{7}{9}x^2 - \frac{56}{9}x - \frac{76}{9}$

Q9: What is x if $f(x) = 7$? or $y = 7$

$f(x) = x$

$7 = x$

so $x = 7$

Q10: What is x if $g(x) = 18$? or $y = 18$

$g(x) = -3x + 3$

$18 = -3x + 3$

$3 \quad -3$

$15 = -3x$

$\div (-3) \quad \div (-3)$

$-5 = x$

so $x = -5$

Q11: What is x if $g(x) = 10$?

$g(x) = -3x + 3$

$10 = -3x + 3$

$-3 \quad -3$

$7 = -3x$

$\div (-3) \quad \div (-3)$

$-\frac{7}{3} = x$

so $x = -\frac{7}{3}$

Q12: What is x if $g(x) = 20$?

$g(x) = -3x + 3$

$20 = -3x + 3$

$-3 \quad -3$

$17 = -3x$

$\div (-3) \quad \div (-3)$

$-\frac{17}{3} = x$

so $x = -\frac{17}{3}$

Q13: What is x if $h(x) = 0$?

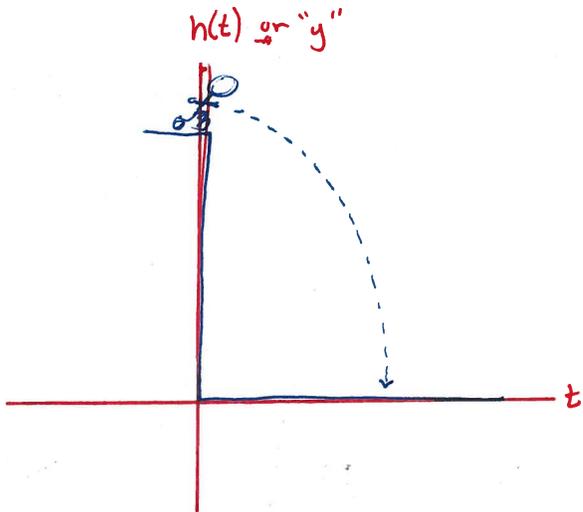
(Hint: You'll need to look at the graph on Pg 3... you can't do this algebraically until Ma20-1 or Ma20-2)

Two answers! $x \approx -6$ and -1.8

Part 5 – Problem Solving

The height of a diver on a board can be described by the function $h(t) = 32 - 4.905t^2$, where h is the diver's height above the water, in metres, t seconds after jumping off the board.

- Determine the diver's height after 1.5 s.
- Estimate how long the diver is in the air.
- Determine an appropriate domain and range.



$$\begin{aligned} \textcircled{A} \quad h(t) &= 32 - 4.905(t)^2 \\ h(1.5) &= 32 - 4.905(1.5)^2 \\ &= 32 - 4.905(2.25) \\ &= 32 - 11.03625 \\ &= 20.96375 \text{ m} \end{aligned}$$

$$\begin{aligned} \textcircled{B} \quad h(t) &= 32 - 4.905t^2 \\ 0 &= 32 - 4.905t^2 \\ -32 & \quad -32 \\ -32 &= (-4.905)t^2 \\ \div(-4.905) & \quad \div(-4.905) \\ 6.52395\dots &= t^2 \\ 2.55 &\approx t \\ \text{So approx } 2.55 \text{ seconds.} \end{aligned}$$

$$\begin{aligned} \textcircled{C} \quad \text{Domain: } & \{t \mid 0 \leq t \leq 2.55, t \in \mathbb{R}\} \\ \text{Range: } & \{h \mid 0 \leq h \leq 32, h \in \mathbb{R}\} \end{aligned}$$

Part 6 – Textbook Practice