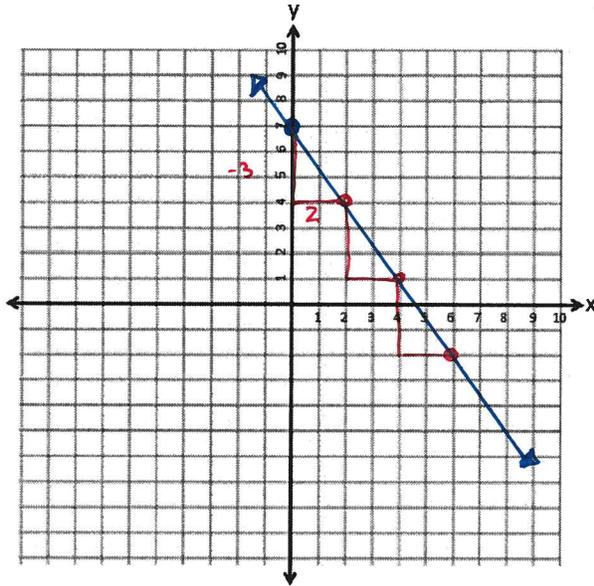


1.47 - 8.1 Graphing Linear Systems of Equations

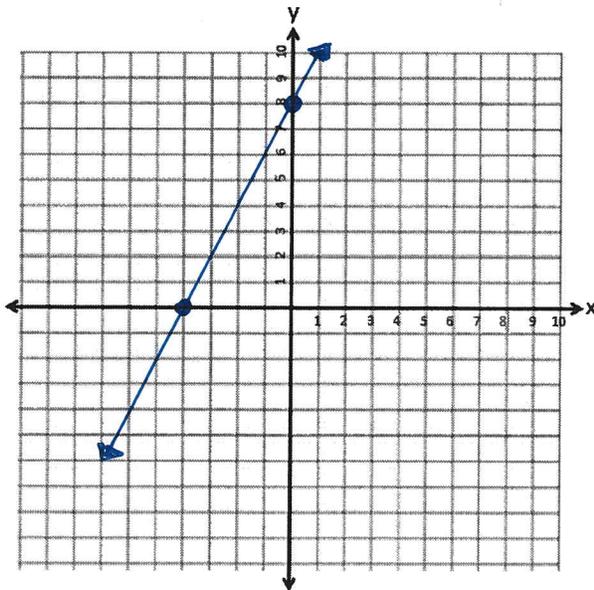
Part 1 - Graphing Slope y-Intercept Form ($y=mx+b$)

Q1: Graph the line $y = -\frac{3}{2}x + 7$



Part 2 - Graphing General Form ($Ax+By+C=0$)

Q2: Graph the line $4x - 2y + 16 = 0$



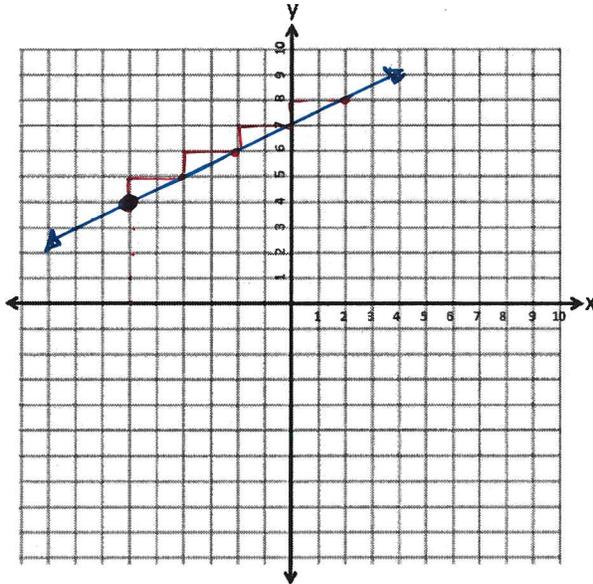
x-int (set y=0)
 $4x + 16 = 0$
 $4x = -16$
 $x = -4$

y-int (set x=0)
 $-2y + 16 = 0$
 $-2y = -16$
 $y = 8$

or
 $4x - 2y + 16 = 0$
 $\quad +2y \quad +2y$
 $4x + 16 = 2y$
 $\div 2 \quad \div 2 \quad \div 2$
 $2x + 8 = y$
 $y = 2x + 8$

Part 3 – Graphing Slope-Point Form $(y - y_1) = m(x - x_1)$ Q3: Graph the line $(y - 4) = \frac{1}{2}(x + 6)$

$$(y - 4) = \frac{1}{2}(x - -6) \quad \text{Point } (-6, 4)$$



or

$$(y - 4) = \frac{1}{2}(x + 6)$$

$$y - 4 = \frac{1}{2}x + 3$$

+4 +4

$$\boxed{y = \frac{1}{2}x + 7}$$

Part 4 – Solutions to System of Equations

System of Linear Equations: Two or more linear equations involving common variables.

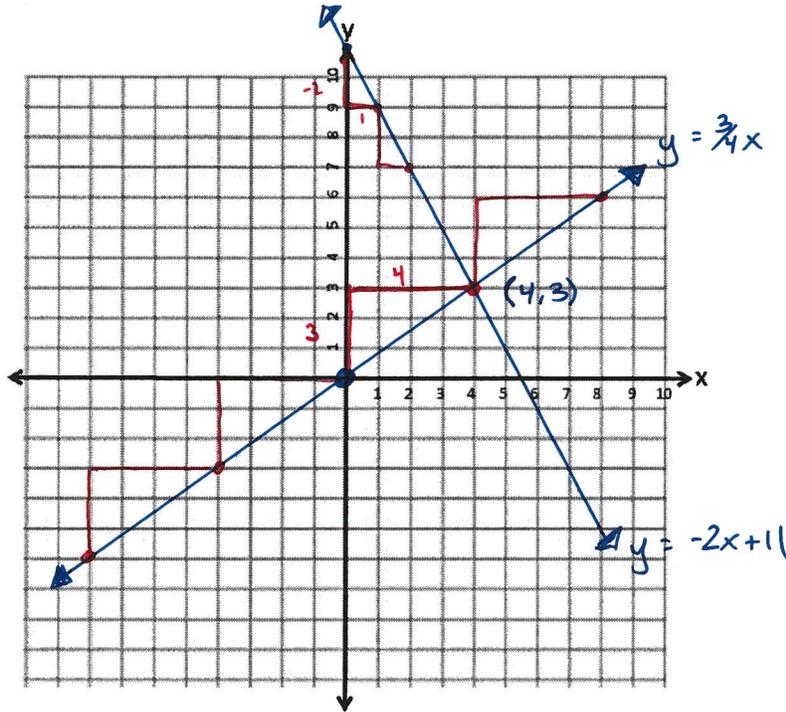
Solution(to a system of linear equations):

- A point of intersection of the lines on a graph.
- An ordered pair that satisfies both equations.

Q4: Given the lines $y = \frac{3}{4}x$ and $y = -2x + 11$, which of the following points is a solution to the system of equations?

| (4,3) | (2,7) |
|---|--|
| $y = \frac{3}{4}x$ $y = \frac{3}{4}(4)$ $y = 3$ | $y = -2x + 11$ $y = -2(2) + 11$ $y = -4 + 11$ $y = 7$ |
| <p>When $x = 4$, both equations give $y = 3$.</p> <p>Both equations have the point $(4, 3)$.</p> | <p>When $x = 2$, the first eqn gives $y = \frac{3}{2}$, so point $(2, \frac{3}{2})$.</p> <p>When $x = 2$, the second eqn gives $y = 7$, so point $(2, 7)$.</p> <p><u>Not</u> the same point, so <u>not</u> a soln.</p> |

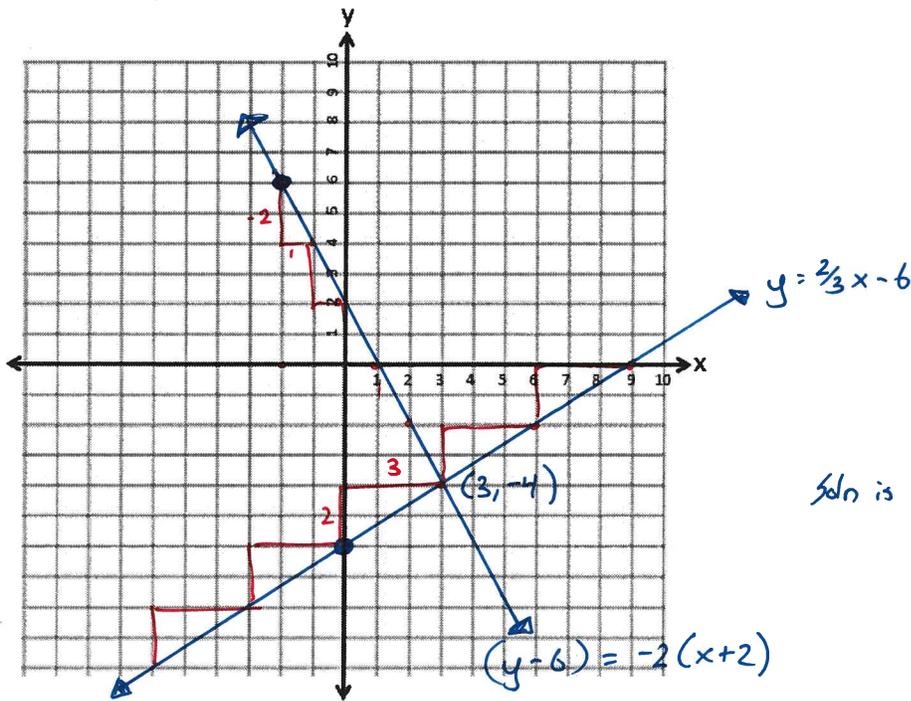
Q5: Graph the lines $y = \frac{3}{4}x$ and $y = -2x + 11$ to confirm the solution to the system of equations.



Soln is $(4, 3)$

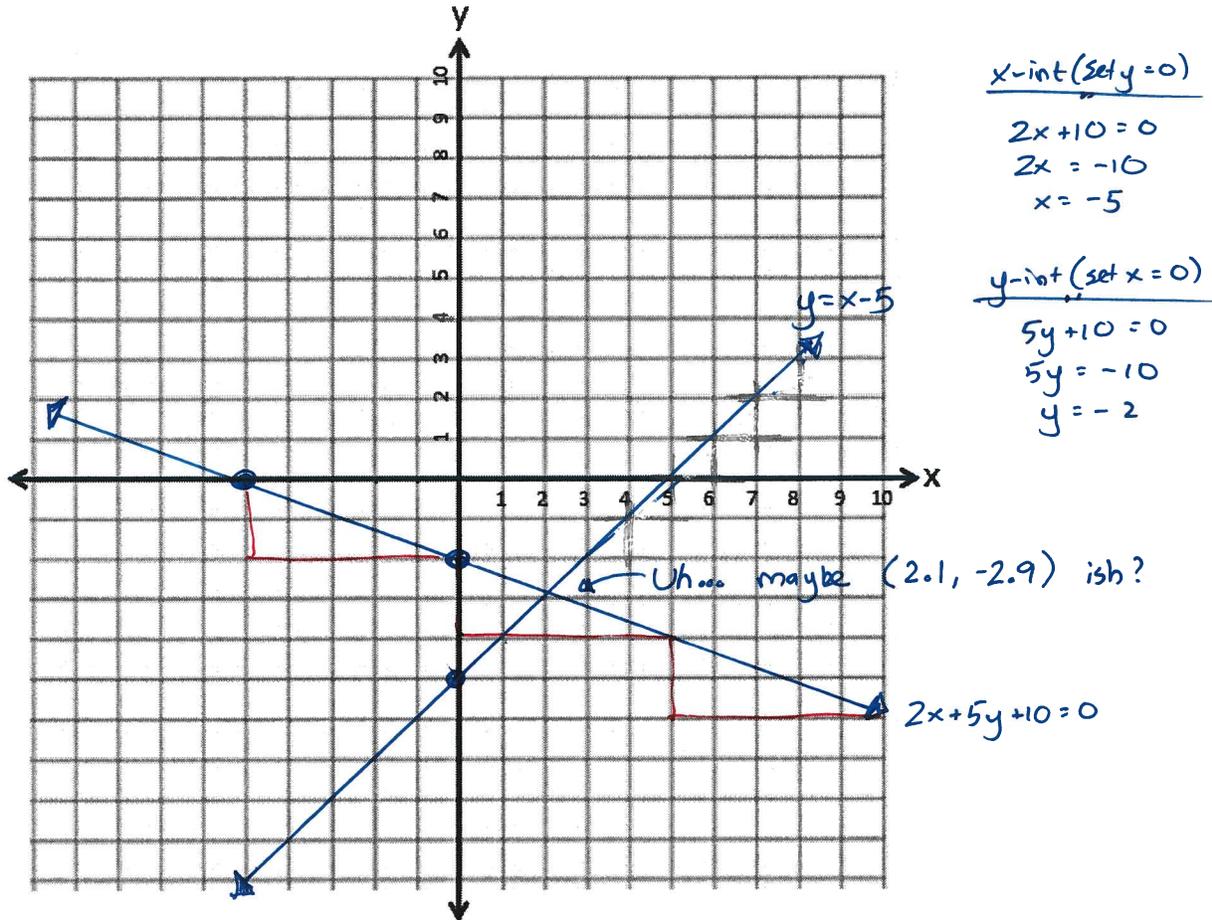
Q6: Graph the lines $(y - 6) = -2(x + 2)$ and $y = \frac{2}{3}x - 6$ to determine the solution to the system of equations.

$$(y - 6) = -\frac{2}{1}(x - -2)$$



Soln is $(3, -4)$

Q7: Graph the lines $2x + 5y + 10 = 0$ and $y = x - 5$ to determine the solution to the system of equations.



Q8: Confirm your answer to Q7 by checking to see if the point exists on each line.

$$2(x) + 5y + 10 = 0$$

$$2(2.1) + 5y + 10 = 0$$

$$4.2 + 5y + 10 = 0$$

$$14.2 + 5y = 0$$

$$5y = -14.2$$

$$y \approx -2.84$$

$$y = (x) - 5$$

$$y = (2.1) - 5$$

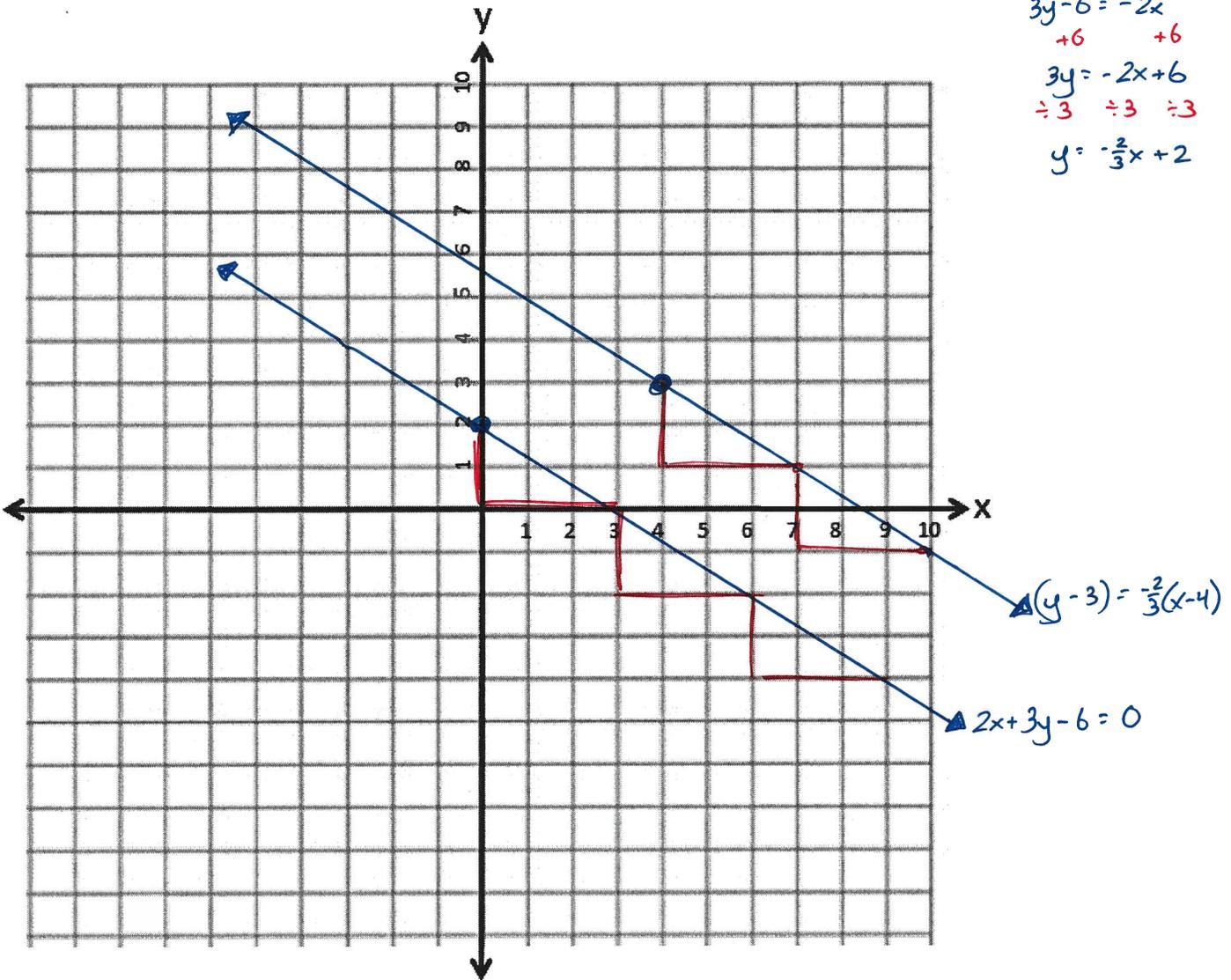
$$y \approx -2.9$$

So not exactly the point of intersection, but pretty close.

We'll learn how to do this exactly with algebra next lesson.

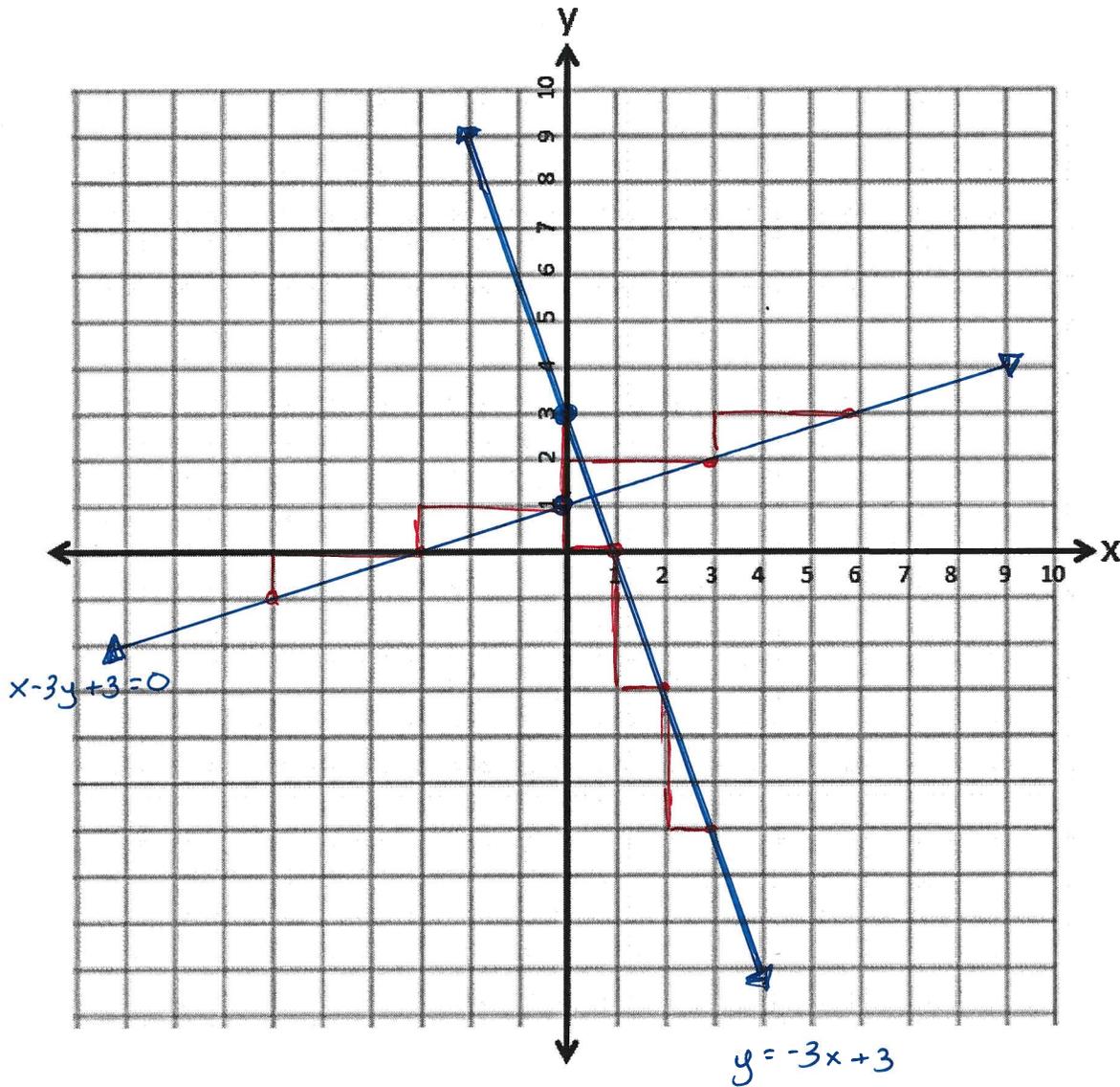
Q9: Graph the lines $(y - 3) = -\frac{2}{3}(x - 4)$ and $2x + 3y - 6 = 0$ to determine the solution to the system of equations.

$$\begin{aligned} 2x + 3y - 6 &= 0 \\ -2x & \quad -2x \\ 3y - 6 &= -2x \\ +6 & \quad +6 \\ 3y &= -2x + 6 \\ \div 3 & \quad \div 3 \quad \div 3 \\ y &= -\frac{2}{3}x + 2 \end{aligned}$$



Parallel lines never cross.
No solution.

Q10: Graph the lines $x - 3y + 3 = 0$ and $y = -3x + 3$ to determine the solution to the system of equations.



$$\begin{aligned}x - 3y + 3 &= 0 \\+ 3y &+ 3y \\x + 3 &= 3y \\ \div 3 &\div 3 \div 3 \\ \frac{1}{3}x + 1 &= y \\ y &= \frac{1}{3}x + 1\end{aligned}$$

Soln is approx $(0.5, 1.3)$