

1.67 - 1.28 - 1.2 Arithmetic Sequences and Series

Use the following information to answer Q1:

An Arithmetic Sequence is shown below:

$$\begin{array}{c} -3 \quad -3 \\ \curvearrowright \quad \curvearrowright \\ 26, 23, 20, 17, \dots \end{array}$$

Q1: Determine the 15<sup>th</sup> term in the sequence. (2 marks)

$$t_n = t_1 + (n-1)d$$

$$t_n = 26 + (n-1)(-3)$$

$$t_{15} = 26 + (15-1)(-3)$$

$$t_{15} = 26 + (14)(-3)$$

$$t_{15} = -16$$

Use the following information to answer Q2:

The 25<sup>th</sup> term of an Arithmetic Sequence is 19. The 34<sup>th</sup> term is -44.Q2: What is the 400<sup>th</sup> term in the sequence? (3 marks)

$$n = \frac{y_2 - y_1}{x_2 - x_1} = \frac{(-44) - (19)}{34 - 25} = \frac{-63}{9} = -7$$

$$d = -7$$

$$t_n = t_1 + (n-1)d \quad \text{Use 25<sup>th</sup> term is 19}$$

$$19 = t_1 + (25-1)(-7)$$

$$19 = t_1 + (24)(-7)$$

$$187 = t_1$$

$$t_n = t_1 + (n-1)d$$

$$t_{400} = 187 + (400-1)(-7)$$

$$t_{400} = -2606$$

Use the following information to answer Q3:

An Arithmetic Sequence is shown below:

$$\begin{array}{ccccccc}
 & & +15 & & +15 & & +15 \\
 & \nearrow & & \nearrow & & \nearrow & \\
 -5 & + & 10 & + & 25 & + & 40 + \dots
 \end{array}$$

Q3: What is the sum of the first 40 terms? (2 marks)

$$d = +15 \quad t_1 = -5$$

$$S_n = \frac{n}{2} [2t_1 + (n-1)d]$$

$$S_{40} = \frac{40}{2} [2(-5) + (40-1)(15)]$$

$$S_{40} = 20 [-10 + 585]$$

$$S_{40} = 11,500$$

**MARKING:**

Beginning	0.0 – 3.0
Progressing	3.5 – 5.0
Competent	5.5 – 6.5
Exemplary	7.0