

First Name: _____

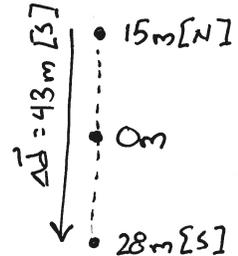
Last Name: _____

107 - Worksheet - Motion in 1-Dimension

/ 30 marks

Part 1: Uniform Motion Equation

$$\vec{v}_{\text{ave}} = \frac{\Delta \vec{d}}{\Delta t}$$



Use the following information to answer Q1 – Q5:

John starts 15m [N] of his house and runs until he is 28 m [S] of his house. This run takes him 50 seconds.

Q1: John ran a total distance of $a.bc \times 10^d$ m, where a , b , c , and d are __, __, __, and __.

(Record your **four digit** answer in the Numerical Response boxes below)

4	3	0	1
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$$\begin{aligned} d &= 43 = 4.30 \times 10^1 \\ &= a.bc \times 10^d \end{aligned}$$

Q2: Which of the following best describes John's initial position?

- a. $\vec{d}_i = 13\text{m [S]}$
- b. $\vec{d}_i = 15\text{m [N]}$
- c. $\vec{d}_i = 28\text{m [S]}$
- d. $\vec{d}_i = 43\text{m [S]}$

Q3: Which of the following best describes John's final position?

- a. $\vec{d}_f = 13\text{m [S]}$
- b. $\vec{d}_f = 15\text{m [N]}$
- c. $\vec{d}_f = 28\text{m [S]}$
- d. $\vec{d}_f = 43\text{m [S]}$

KEY

Q4: Which equation best models how to calculate John's displacement?

- a. $\Delta \vec{d} = 15\text{m} [N] + 28\text{m}[N]$
- b. $\Delta \vec{d} = -28\text{m} [N] + 15\text{m}[N]$
- c. $\Delta \vec{d} = -28\text{m} [N] - 15\text{m}[N]$ \longrightarrow
- d. $\Delta \vec{d} = 28\text{m} [N] - 15\text{m} [N]$
- $$\begin{aligned} \Delta \vec{d} &= \vec{d}_f - \vec{d}_i \\ &= 28\text{m}[S] - 15\text{m}[N] \\ &= -28\text{m}[N] - 15\text{m}[N] \\ &= -43\text{m}[N] \text{ or } 43\text{m}[S] \end{aligned}$$

Q5: John's velocity is $a.bc \times 10^{-d}$ m/s, where a , b , c , and d are __, __, __, and __.

(Record your four digit answer in the Numerical Response boxes below)

8	6	0	1
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$$\begin{aligned} \vec{v} &= \frac{\Delta \vec{d}}{\Delta t} = \frac{43\text{m}[S]}{50\text{s}} = 0.86\text{m/s}[S] \\ &= 8.60 \times 10^{-1}\text{m/s} \\ &= a.bc \times 10^{-d} \end{aligned}$$

Q6: A rabbit is 15m [E] of a rabbit hole when initially, then runs to 24m [E]. This total run takes place in 4 seconds. What is the rabbit's velocity? (3 marks)

$$\begin{aligned} \vec{d}_i &= 15\text{m}[E] \\ \vec{d}_f &= 24\text{m}[E] \\ \Delta \vec{d} &= ? \\ t &= 4\text{s} \\ \vec{v} &= ? \end{aligned}$$

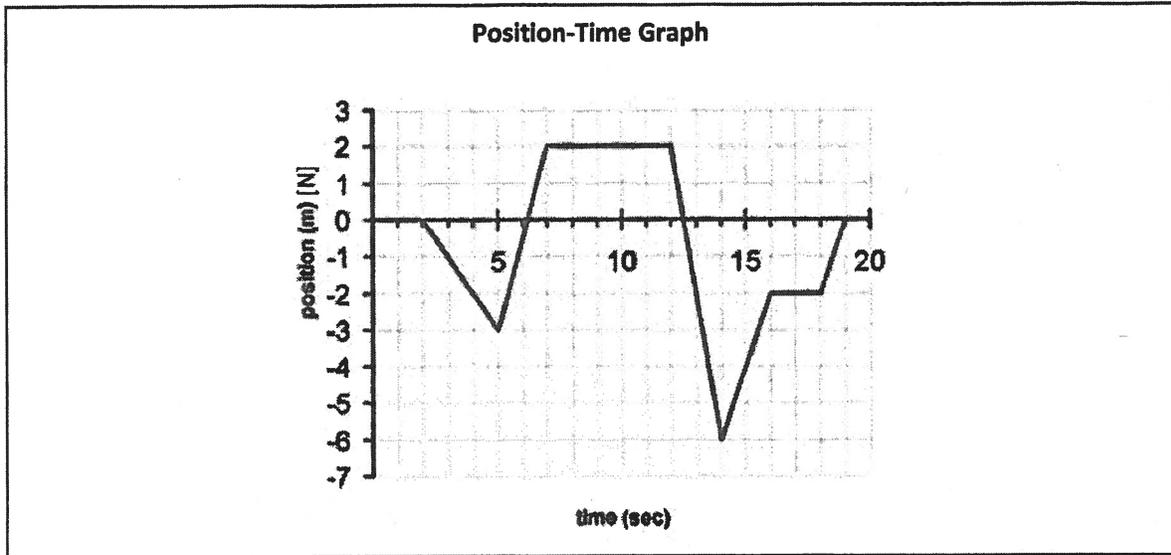
$$\begin{aligned} \Delta \vec{d} &= \vec{d}_f - \vec{d}_i \\ &= 24\text{m}[E] - 15\text{m}[E] \\ &= 9\text{m}[E] \end{aligned}$$

$$\vec{v} = \frac{\Delta \vec{d}}{\Delta t} = \frac{9\text{m}[E]}{4\text{s}}$$

$$\vec{v} = 2.25\text{m/s}[E]$$

Part 2: Interpreting Position-Time Graphs

Use the following information to answer Q7 – Q14:



Q7: During what time period(s) is the object north of the origin?

- a. 5 - 7s, 14 - 16s, 18 - 19s
- b. 6 - 12.5s
- c. 0 - 2s, 7 - 12s, 16 - 18s, 19 - 20s
- d. 2 - 5s, 12 - 14s

When position (y axis value) is above the "zero" line (x-axis)

Q8: During what time period(s) is the object moving north?

- e. 5 - 7s, 14 - 16s, 18 - 19s
- f. 6 - 12.5s
- g. 0 - 2s, 7 - 12s, 16 - 18s, 19 - 20s
- h. 2 - 5s, 12 - 14s

When velocity (slope) is positive.

Q9: During what time period(s) is the object stationary?

- a. 5 - 7s, 14 - 16s, 18 - 19s
- b. 6 - 12.5s
- c. 0 - 2s, 7 - 12s, 16 - 18s, 19 - 20s
- d. 2 - 5s, 12 - 14s

When velocity (slope) is zero
When position (y-value) isn't changing.

KEY

Q10: What is the magnitude of the velocity between 5 and 7 seconds?

(Record your three digit answer in the Numerical Response boxes below)

2	.	5	0
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$$\vec{v} = \frac{\Delta \vec{d}}{\Delta t} = \frac{5 \text{ m [N]}}{2 \text{ s}} = 2.5 \text{ m/s [N]}$$

Q11: What is the magnitude of the acceleration of the object between 12 and 14 seconds?

(Record your three digit answer in the Numerical Response boxes below)

0	.	0	0
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Constant velocity (slope)? No acceleration!

Q12: During what time period(s) is the object south of the origin?

2-6 s
12.5-19 s

Q13: During what time period(s) is the object moving south?

2-5 s
12-14 s

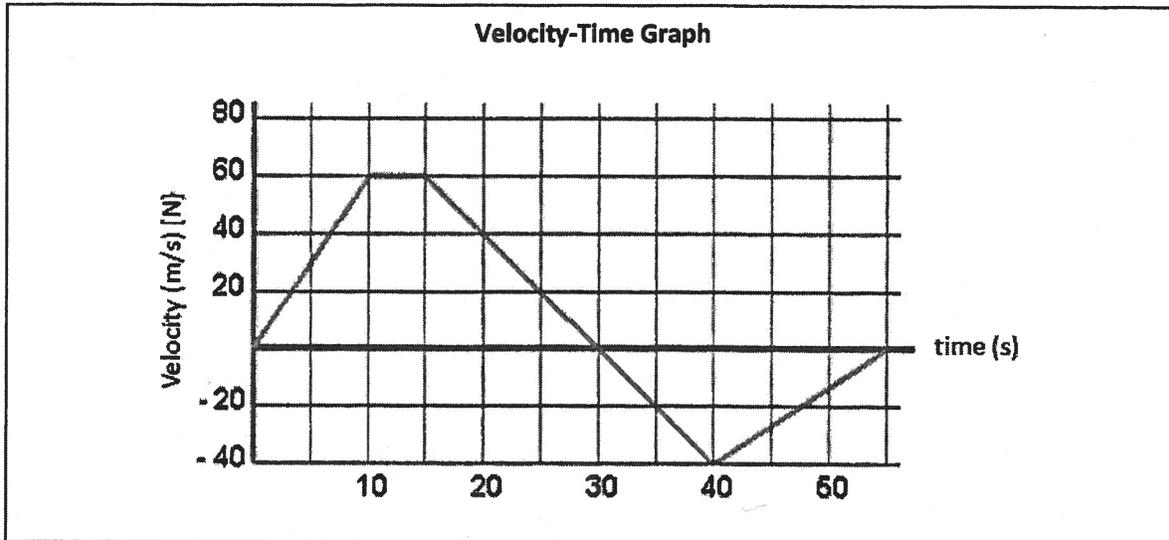
Q14: The displacement of the object between 14 and 16 seconds is

- a. 4 m [N]
- b. 4 m [S]
- c. 8 m [N]
- d. 8 m [S]

$$\begin{aligned} \Delta \vec{d} &= \vec{d}_f - \vec{d}_i \\ &= -2 \text{ m [N]} - (-6 \text{ m [N]}) \\ &= -2 + 6 \\ &= 4 \text{ m [N]} \end{aligned}$$

Part 3: Interpreting Velocity-Time Graphs

Use the following information to answer Q15 – Q22:



Q15: During what time period(s) is the object stationary?

- a. 10 – 15s → moving @ 60 m/s
 - b. 55 – 60s
 - c. All of the above
 - d. None of the above
- When velocity (y-value) is zero.*

Q16: During what time period(s) is the object moving north?

- a. 0 – 10s
 - b. 0 – 30s
 - c. 40 – 55s
 - d. Both A and C
- When y-value is positive.*

Q17: During what time period(s) is the object accelerating?

- a. 0 – 10s ✓
 - b. 0 – 30s
 - c. 30 – 40s ✓
 - d. Both A and C
- When velocity is becoming more "non-zero".
When it is speeding up.*

■ KEY ■

Q18: What is the acceleration of the object between 20 and 30 seconds?

$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t} = \frac{-40 \text{ m/s [N]}}{10 \text{ s}} = -4 \text{ m/s}^2 \text{ [N]} \quad \text{or } 4 \text{ m/s}^2 \text{ [S]}$$

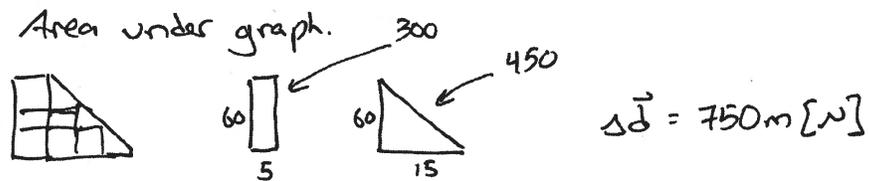
Q19: What is the acceleration of the object between 40 and 55 seconds?

$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t} = \frac{40 \text{ m/s [N]}}{15 \text{ s}} = 2.6 \text{ m/s}^2 \text{ [N]}$$

Q20: What is the velocity of the object at 20 seconds?

y-value is 40 m/s [N]

Q21: What is the displacement of the object between 10 and 30 seconds?



Q22: During what time period(s) is the object decelerating?

when its velocity is becoming closer to zero.

15 - 30s

40 - 55s

KEY

Part 4: Horizontally Accelerated Motion

	$d = v_f t - \frac{1}{2} a t^2$
$\bar{a}_{ave} = \frac{\Delta \vec{v}}{\Delta t}$	$\bar{d} = \left(\frac{\vec{v}_f + \vec{v}_i}{2} \right) t$
$\bar{d} = \vec{v}_i t + \frac{1}{2} \bar{a} t^2$	$v_f^2 = v_i^2 + 2ad$

Q23: A Honda civic can accelerate from a rest to 26.8m/s [S] in 9.8 seconds. How much distance does the Honda Civic cover during this acceleration? (3 marks)

$$\begin{aligned} \vec{v}_i &= 0 \text{ m/s} \\ \vec{v}_f &= 26.8 \text{ m/s [S]} \\ t &= 9.8 \text{ s} \\ d &=? \end{aligned}$$

$$\begin{aligned} \bar{d} &= \left(\frac{\vec{v}_f + \vec{v}_i}{2} \right) t \\ \bar{d} &= \left(\frac{26.8 \text{ m/s [S]} + 0 \text{ m/s [S]}}{2} \right) (9.8 \text{ s}) \\ \bar{d} &= 131.32 \text{ m [S]} \end{aligned}$$

Q24: A stationary object is accelerated at 3.2m/s² [S] for 15m [S]. How much time elapsed? (3 marks)

$$\begin{aligned} \vec{v}_i &= 0 \text{ m/s [S]} \\ \vec{a} &= 3.2 \text{ m/s}^2 \text{ [S]} \\ \vec{d} &= 15 \text{ m [S]} \\ t &=? \end{aligned}$$

$$\begin{aligned} d &= v_i t + \frac{1}{2} a t^2 \\ 15 \text{ m [S]} &= (0 \text{ m/s}) t + \frac{1}{2} (3.2 \text{ m/s}^2 \text{ [S]}) t^2 \\ 15 &= 0t + 1.6 t^2 \\ 15 &= 1.6 t^2 \\ 9.375 &= t^2 \\ t &= 3.06 \text{ s} \end{aligned}$$

Part 5: Vertically Accelerated Motion

$$\vec{d} = \vec{v}_f t - \frac{1}{2} \vec{a} t^2$$

$$\vec{d}_{\text{ave}} = \frac{\Delta \vec{v}}{\Delta t} \quad \vec{d} = \left(\frac{\vec{v}_f + \vec{v}_i}{2} \right) t$$

$$\vec{d} = \vec{v}_i t + \frac{1}{2} \vec{a} t^2 \quad v_f^2 = v_i^2 + 2ad$$

Use the following information to answer Q25 to Q27:

A ball at ground level is shot vertically upward at 2m/s.

Q25: The ball reaches a maximum height of $a.bc \times 10^d$ m, where $a, b, c,$ and d are , , , and .

(Record your **four digit** answer in the Numerical Response boxes below)

2	0	4	1
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$$v_i = 2 \text{ m/s}$$

$$a = -9.81 \text{ m/s}^2$$

$$d_{\text{max}} = ?$$

$$v_f = 0 \text{ m/s @ top}$$

$$v_f^2 = v_i^2 + 2ad$$

$$0^2 = (2)^2 + 2(-9.81)d$$

$$0 = 4 - 19.62d$$

$$19.62d = 4$$

$$d = 0.2038 \text{ m}$$

$$d = 0.2038 \text{ m}$$

$$= 2.038 \times 10^{-1}$$

$$= 2.04 \times 10^{-1}$$

Q26: The ball has a total flight time of $a.bc \times 10^d$ s, where $a, b, c,$ and d are , , , and .

(Record your **four digit** answer in the Numerical Response boxes below)

4	0	8	1
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$$v_i = 2 \text{ m/s}$$

$$a = -9.81 \text{ m/s}^2$$

$$d = 0 \text{ m @ bottom}$$

$$t = ?$$

$$d = v_i t + \frac{1}{2} a t^2$$

$$0 = 2t + \frac{1}{2}(-9.81)t^2$$

$$0 = 2t - 4.905t^2$$

$$\div t \quad \div t \quad \div t$$

$$0 = 2 - 4.905t$$

$$4.905t = 2$$

$$t = 0.4077 \text{ s}$$

$$t = 4.08 \times 10^{-1} \text{ s}$$

Q27: How fast is the ball moving at $t=0.36$ seconds, in meters per second?

(Record your **three digit** answer in the Numerical Response boxes below)

1	.	5	3
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$$v_i = 2 \text{ m/s}$$

$$a = -9.81 \text{ m/s}^2$$

$$t = 0.36 \text{ s}$$

$$v_f = ?$$

$$a = \frac{v_f - v_i}{t}$$

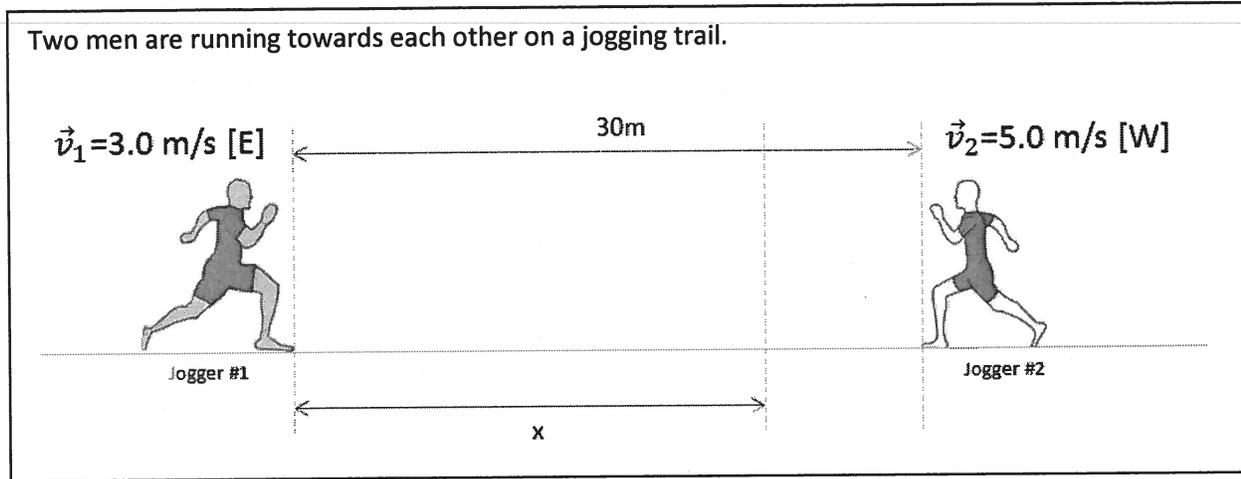
$$(-9.81) = \frac{v_f - (2)}{(0.36)}$$

$$-3.5316 = v_f - 2$$

$$v_f = -1.53 \text{ m/s}$$

Part 6: Harder Questions

Use the following information to answer Q28:



Q28: How far from Jogger #1's original position to they meet, measured in meters?

(Record your **three digit** answer in the Numerical Response boxes below)

1	1	.	3
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Jogger #1

$$v = \frac{d}{t}$$

$$t = \frac{d}{v}$$

$$t = \frac{x}{3}$$

Jogger #2

$$v = \frac{d}{t}$$

$$t = \frac{d}{v}$$

$$t = \frac{30-x}{5}$$

$$t_1 = t_2$$

$$\frac{x}{3} = \frac{30-x}{5}$$

$$5x = 3(30-x)$$

$$5x = 90 - 3x$$

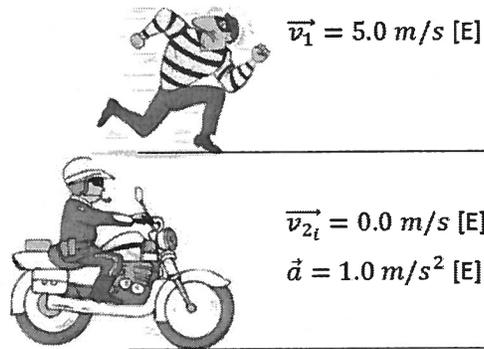
$$8x = 90$$

$$x = 11.25 \text{ m}$$

$$\approx 11.3 \text{ m}$$

Use the following information to answer Q29:

A criminal is running at a steady 5.0 m/s when he runs up parallel to a police officer. The officer, originally stationary, immediately begins to accelerate at 1.0 m/s².



Q29: How many seconds does it take the police officer to catch up to the criminal again?

(Record your three digit answer in the Numerical Response boxes below)

1	0	.	0
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Criminal

$$v = \frac{d}{t}$$

$$d = vt$$

$$d = 5t$$

Police Officer

$$d = v_i t + \frac{1}{2} a t^2$$

$$d = (0)t + \frac{1}{2}(1)t^2$$

$$d = 0.5t^2$$

$$d_1 = d_2$$

$$5t = 0.5t^2$$

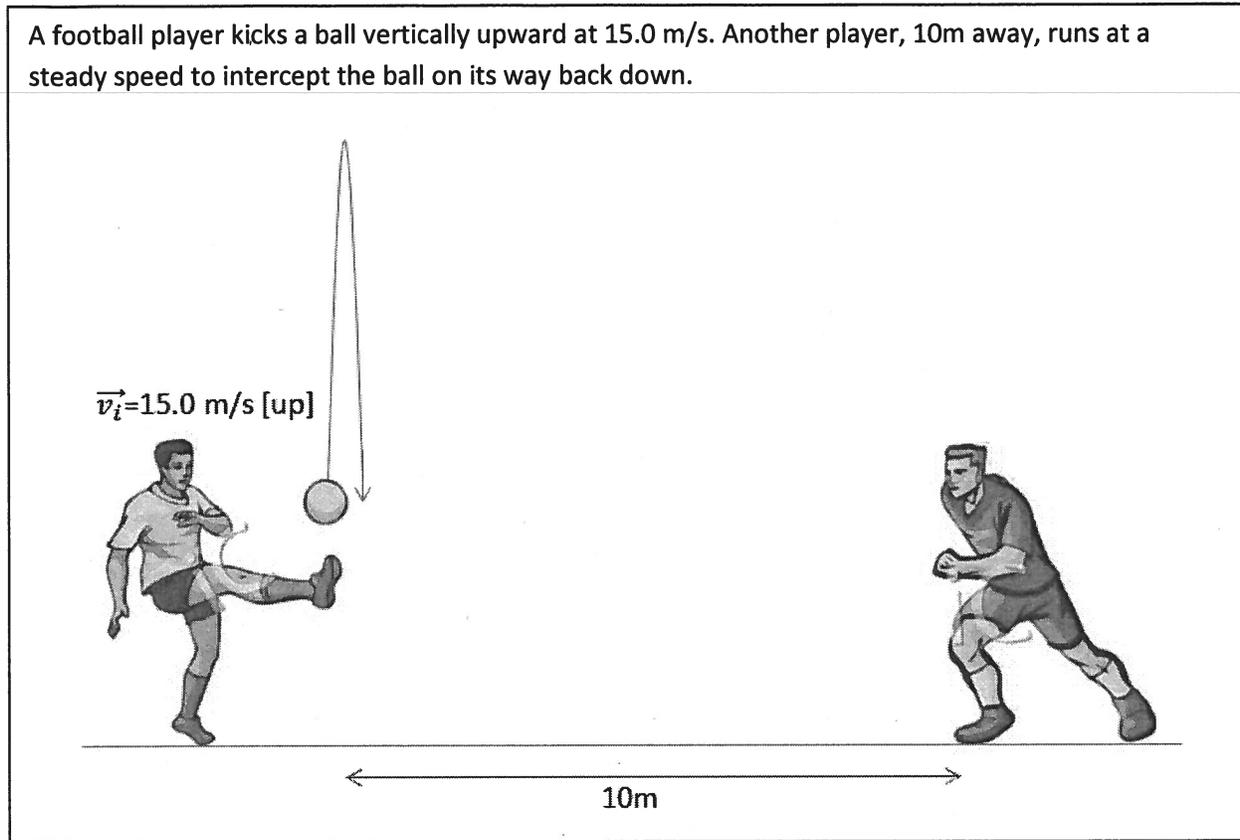
$$\div t \quad \div t$$

$$5 = 0.5t$$

$$10 = t$$

$$t = 10.0 \text{ s}$$

Use the following information to answer Q30:



Q30: If the second player intercepts the ball at exactly the height it was originally launched upward at, how fast what the second player running, in meters per second?

(Record your **three digit** answer in the Numerical Response boxes below)

3	.	2	7
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Ball

$$d = v_i t + \frac{1}{2} a t^2$$

$$0 = (15)t + \frac{1}{2}(-9.81)t^2$$

$$0 = 15t - 4.905t^2$$

$$\div t \quad \div t \quad \div t$$

$$0 = 15 - 4.905t$$

$$4.905t = 15$$

$$t = 3.058s$$

Player #2

$$v = \frac{d}{t}$$

$$v = \frac{10m}{3.058s}$$

$$v = 3.269 \text{ m/s}$$

$$v \approx 3.27 \text{ m/s}$$