

First Name: \_\_\_\_\_

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## L12 - FQ - Springs

Use the following information to answer Q1-Q2:

A spring of unknown spring constant is attached to a mass of 3kg and stretched a maximum distance of 10m. When it is released, it speeds up, reaching a maximum speed of 2m/s at the equilibrium position, before returning to its original position.

**Q1:** The spring constant of this spring is  $a.bc \times 10^d$  N/m, where  $a$ ,  $b$ ,  $c$ , and  $d$  are \_\_\_\_, \_\_\_\_, \_\_\_\_, and \_\_\_\_.

(Record your **four digit** answer in the Numerical Response boxes below)

1	2	0	1
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$$\begin{aligned}
 E_p &\rightarrow E_k \\
 \frac{1}{2}kx^2 &= \frac{1}{2}mv^2 \\
 \frac{1}{2}k(10)^2 &= \frac{1}{2}(3)(2)^2 \\
 \frac{1}{2}(k)(100) &= 6 \\
 k &= 0.12 \text{ N/m} \\
 k &= 1.20 \times 10^{-1} \text{ N/m}
 \end{aligned}$$

**Q2:** The frequency of oscillation is

- a.  $3.18 \times 10^{-2}$  Hz
- b.  $7.96 \times 10^{-1}$  Hz
- c. 1.26 Hz
- d.  $3.14 \times 10^1$  Hz

$$\begin{aligned}
 T &= 2\pi \sqrt{\frac{m}{k}} = 2\pi \sqrt{\frac{3}{0.12}} \\
 &= 2\pi \sqrt{25} \\
 &= 31.4159 \text{ s}
 \end{aligned}$$

$$f = \frac{1}{T} = \frac{1}{31.4159} = 3.18 \times 10^{-2} \text{ Hz}$$

■ KEY ■

Q3: Algebraically rearrange the equation  $T = 2\pi\sqrt{\frac{m}{k}}$  to solve for  $k$ . Simplify your expression. (2 marks)

$$T = 2\pi\sqrt{\frac{m}{k}}$$

$$\div 2\pi \quad \div 2\pi$$

$$\frac{T}{2\pi} = \sqrt{\frac{m}{k}}$$

$$\frac{T^2}{4\pi^2} = \frac{m}{k}$$

$$\times k \quad \times k$$

$$\frac{kT^2}{4\pi^2} = m$$

$$\times 4\pi^2 \quad \times 4\pi^2$$

$$kT^2 = 4\pi^2 m$$

$$\div T^2 \quad \div T^2$$

$$k = \frac{4\pi^2 m}{T^2}$$

**MARKING:**

Beginning	0 - 1.5
Progressing	2 - 2.5
Competent	3 - 3.5
Exemplary	4