

■ L61 - WORKSHEET - ADDING, SUBTRACTING, MULTIPLYING AND DIVIDING. ■

■ KEY ■

Simplify.

$$1) 3\sqrt{6} - 4\sqrt{6} - \sqrt{6}$$

$$2) -3\sqrt{7} + 4\sqrt{7} - \sqrt{7}$$

$$3) -11\sqrt{21} - 11\sqrt{21} - 22\sqrt{21}$$

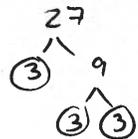
$$4) -9\sqrt{15} + 10\sqrt{15} - \sqrt{15}$$

$$5) -10\sqrt{7} + 12\sqrt{7} - 2\sqrt{7}$$

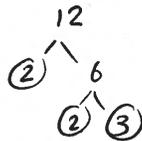
$$6) -3\sqrt{17} - 4\sqrt{17} - 7\sqrt{17}$$

$$7) -10\sqrt{11} - 11\sqrt{11} - 21\sqrt{11}$$

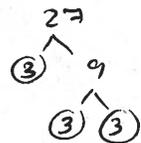
$$8) -2\sqrt{3} + 3\sqrt{27} - 2\sqrt{3} + 3\sqrt{3^2 \cdot 3} - 2\sqrt{3} + 3 \cdot 3\sqrt{3} - 2\sqrt{3} + 9\sqrt{3} - 7\sqrt{3}$$



$$9) -\sqrt{12} + 3\sqrt{3} - \sqrt{2^2 \cdot 3} + 3\sqrt{3} - 2\sqrt{3} + 3\sqrt{3} - \sqrt{3}$$



$$10) 3\sqrt{3} - \sqrt{27} - 3\sqrt{3} - \sqrt{3^2 \cdot 3} - 3\sqrt{3} - 3\sqrt{3} - \emptyset$$



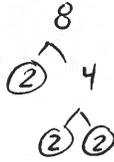
11) $3\sqrt{8} + 3\sqrt{2}$

$3\sqrt{2^2 \cdot 2} + 3\sqrt{2}$

$3 \cdot 2\sqrt{2} + 3\sqrt{2}$

$6\sqrt{2} + 3\sqrt{2}$

$9\sqrt{2}$



12) $-3\sqrt{6} + 3\sqrt{6}$

\emptyset

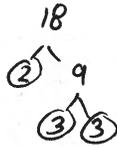
13) $3\sqrt{18} - 2\sqrt{2}$

$3\sqrt{2 \cdot 3^2} - 2\sqrt{2}$

$3 \cdot 3\sqrt{2} - 2\sqrt{2}$

$9\sqrt{2} - 2\sqrt{2}$

$7\sqrt{2}$



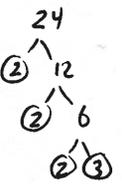
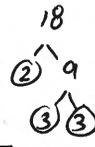
14) $-3\sqrt{18} + 3\sqrt{8} - \sqrt{24}$

$-3\sqrt{2 \cdot 3^2} + 3\sqrt{2 \cdot 2^2} - \sqrt{2^2 \cdot 2 \cdot 3}$

$-3 \cdot 3\sqrt{2} + 3 \cdot 2\sqrt{2} - 2\sqrt{2 \cdot 3}$

$-9\sqrt{2} + 6\sqrt{2} - 2\sqrt{6}$

$-3\sqrt{2} - 2\sqrt{6}$



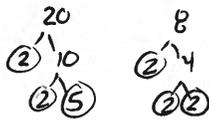
15) $-3\sqrt{2} + 3\sqrt{20} - 3\sqrt{8}$

$-3\sqrt{2} + 3\sqrt{2^2 \cdot 5} - 3\sqrt{2^2 \cdot 2}$

$-3\sqrt{2} + 3 \cdot 2\sqrt{5} - 3 \cdot 2\sqrt{2}$

$-3\sqrt{2} + 6\sqrt{5} - 6\sqrt{2}$

$-9\sqrt{2} + 6\sqrt{5}$

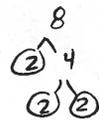


16) $-3\sqrt{3} - \sqrt{8} - 3\sqrt{3}$

$-3\sqrt{3} - \sqrt{2^2 \cdot 2} - 3\sqrt{3}$

$-3\sqrt{3} - 2\sqrt{2} - 3\sqrt{3}$

$-6\sqrt{3} - 2\sqrt{2}$

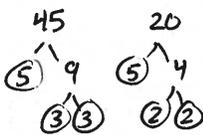


17) $-\sqrt{45} + 2\sqrt{5} - \sqrt{20} - 2\sqrt{6}$

$-\sqrt{3^2 \cdot 5} + 2\sqrt{5} - \sqrt{2^2 \cdot 5} - 2\sqrt{6}$

$-3\sqrt{5} + 2\sqrt{5} - 2\sqrt{5} - 2\sqrt{6}$

$-3\sqrt{5} - 2\sqrt{6}$



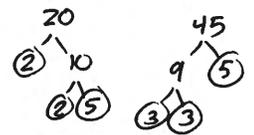
18) $2\sqrt{20} - \sqrt{20} + 3\sqrt{20} - 2\sqrt{45}$

$2\sqrt{2^2 \cdot 5} - \sqrt{2^2 \cdot 5} + 3\sqrt{2^2 \cdot 5} - 2\sqrt{3^2 \cdot 5}$

$2 \cdot 2\sqrt{5} - 2\sqrt{5} + 3 \cdot 2\sqrt{5} - 2 \cdot 3\sqrt{5}$

$4\sqrt{5} - 2\sqrt{5} + 6\sqrt{5} - 6\sqrt{5}$

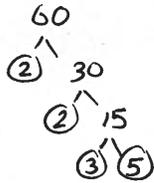
$2\sqrt{5}$



$$19) \sqrt[3]{3} \cdot \sqrt[3]{-20}$$

$$\sqrt[3]{-60}$$

$$-\sqrt[3]{60}$$



$$20) \sqrt{5} \cdot \sqrt{3}$$

$$\sqrt{15}$$

$$21) 3\sqrt{3}(4-3\sqrt{5})$$

$$12\sqrt{3} - 9\sqrt{5}$$

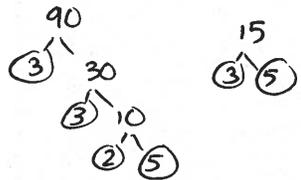
$$22) 4\sqrt{15}(-3\sqrt{6}+5)$$

$$-12\sqrt{90} + 20\sqrt{15}$$

$$-12\sqrt{3^2 \cdot 2 \cdot 5} + 20\sqrt{3 \cdot 5}$$

$$-12 \cdot 3\sqrt{2 \cdot 5} + 20\sqrt{3 \cdot 5}$$

$$-36\sqrt{10} + 20\sqrt{15}$$



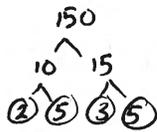
$$23) \sqrt{15}(2\sqrt{10}-4\sqrt{6})$$

$$2\sqrt{150} - 4\sqrt{90}$$

$$2\sqrt{2 \cdot 3 \cdot 5^2} - 4\sqrt{3^2 \cdot 2 \cdot 5}$$

$$2 \cdot 5\sqrt{2 \cdot 3} - 4 \cdot 3\sqrt{2 \cdot 5}$$

$$10\sqrt{6} - 12\sqrt{10}$$



$$24) (-7 + \sqrt{3x})(4 + \sqrt{3x})$$

$$-28 - 7\sqrt{3x} + 4\sqrt{3x} + 3x$$

$$-28 - 3\sqrt{3x} + 3x \quad \text{where } x \geq 0$$

$$25) (\sqrt{3} + \sqrt{5x})(\sqrt{3} - 5\sqrt{5x})$$

$$3 - 5\sqrt{15x} + \sqrt{15x} - 5(5x)$$

$$3 - 5\sqrt{15x} + \sqrt{15x} - 25x$$

$$3 - 4\sqrt{15x} - 25x$$

$$26) (7 + \sqrt{6})(1 + \sqrt{6})$$

$$7 + 7\sqrt{6} + 1\sqrt{6} + 6$$

$$13 + 8\sqrt{6}$$

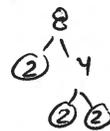
Simplify.

$$27) \frac{\sqrt{15}}{5\sqrt{20}} = \frac{1}{5} \sqrt{\frac{15}{20}} = \frac{1}{5} \sqrt{\frac{3}{4}}$$

$$= \frac{1}{5} \frac{\sqrt{3}}{\sqrt{4}} = \frac{1\sqrt{3}}{5(2)} = \frac{\sqrt{3}}{10}$$

$$28) \frac{\sqrt{8}}{\sqrt{100}} = \frac{\sqrt{8}}{10} = \frac{\sqrt{2^2 \cdot 2}}{10}$$

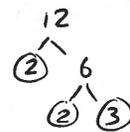
$$= \frac{2\sqrt{2}}{10} = \frac{\sqrt{2}}{5}$$



$$29) \frac{4}{\sqrt{5}} \cdot \frac{\sqrt{5}}{\sqrt{5}} = \frac{4\sqrt{5}}{5}$$

$$30) \frac{\sqrt{4}}{5\sqrt{3}} \cdot \frac{\sqrt{3}}{\sqrt{3}} = \frac{\sqrt{12}}{5(3)} = \frac{\sqrt{2^2 \cdot 3}}{15}$$

$$= \frac{2\sqrt{3}}{15}$$



$$31) \frac{\sqrt{3x^2y^3}}{4\sqrt{5xy^3}} = \frac{1}{4} \sqrt{\frac{3x^2y^3}{5xy^3}} = \frac{1}{4} \sqrt{\frac{3x}{5}}$$

$$= \frac{\sqrt{3x}}{4\sqrt{5}} \cdot \frac{\sqrt{5}}{\sqrt{5}} = \frac{\sqrt{15x}}{4(5)} = \frac{\sqrt{15x}}{20}$$

$$32) \frac{\sqrt{15xy}}{3\sqrt{10xy^3}} = \frac{1}{3} \sqrt{\frac{15xy}{10xy^3}} = \frac{1}{3} \sqrt{\frac{3}{2y^2}}$$

$$= \frac{\sqrt{3}}{3\sqrt{2y^2}} = \frac{\sqrt{3}}{3y\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{\sqrt{6}}{3y(2)}$$

$$= \frac{\sqrt{6}}{6y}$$

$$\begin{aligned}
 33) \frac{4x^3 - 3\sqrt{3x}}{3\sqrt{3x^2}} &= \frac{4x^3 - 3\sqrt{3x}}{3\sqrt{3x^2}} \\
 &= \frac{(4x^3 - 3\sqrt{3x})}{(3x\sqrt{3})} \cdot \frac{\sqrt{3}}{\sqrt{3}} = \frac{4x^3\sqrt{3} - 3(3)\sqrt{x}}{3x(3)} \\
 &= \frac{4x^3\sqrt{3} - 9\sqrt{x}}{9x}
 \end{aligned}$$

$$\begin{aligned}
 34) \frac{\sqrt{5k^4} + 3\sqrt{2k}}{\sqrt{3k^3}} &= \frac{(k^2\sqrt{5} + 3\sqrt{2k})}{(k\sqrt{3k})} \cdot \frac{\sqrt{3k}}{\sqrt{3k}} \\
 &= \frac{k^2\sqrt{15k} + 3\sqrt{6k^2}}{k(3k)} = \frac{k^2\sqrt{15k} + 3k\sqrt{6}}{3k^2} \\
 &= \frac{k\sqrt{15k} + 3\sqrt{6}}{3k}
 \end{aligned}$$

$$\begin{aligned}
 35) \frac{\left(\frac{5}{-3-3\sqrt{3}}\right) \cdot \left(\frac{-3+3\sqrt{3}}{-3+3\sqrt{3}}\right)}{\frac{-15+15\sqrt{3}}{9-9\sqrt{3}+9\sqrt{3}-9(3)}}
 \end{aligned}$$

$$\begin{aligned}
 &= \frac{-15+15\sqrt{3}}{-18} = \frac{(-5+5\sqrt{3})}{(-6)} \cdot \frac{(-1)}{(-1)} \\
 &= \frac{5-5\sqrt{3}}{6}
 \end{aligned}$$

$$\begin{aligned}
 36) \frac{\left(\frac{4}{\sqrt{2}-5\sqrt{3}}\right) \cdot \left(\frac{\sqrt{2}+5\sqrt{3}}{\sqrt{2}+5\sqrt{3}}\right)}{\frac{4\sqrt{2}+20\sqrt{3}}{2+5\sqrt{6}-5\sqrt{6}-25(3)}} &= \frac{4\sqrt{2}+20\sqrt{3}}{-73} \\
 &= \frac{(4\sqrt{2}+20\sqrt{3})}{(-73)} \cdot \frac{(-1)}{(-1)} = \frac{-4\sqrt{2}-20\sqrt{3}}{73}
 \end{aligned}$$

$$37) \frac{\left(\frac{\sqrt{5}+3}{4-\sqrt{5}}\right) \cdot \left(\frac{4+\sqrt{5}}{4+\sqrt{5}}\right)}{\frac{4\sqrt{5}+5+12+3\sqrt{5}}{16+4\sqrt{5}-4\sqrt{5}-5}}$$

$$\begin{aligned}
 &= \frac{7\sqrt{5}+17}{11}
 \end{aligned}$$

$$38) \frac{\left(\frac{3-4\sqrt{3}}{4\sqrt{5}+3\sqrt{2}}\right) \cdot \left(\frac{4\sqrt{5}-3\sqrt{2}}{4\sqrt{5}-3\sqrt{2}}\right)}{\frac{12\sqrt{5}-9\sqrt{2}-16\sqrt{15}+12\sqrt{6}}{16(5)-12\sqrt{10}+12\sqrt{10}-9(2)}}$$

$$\begin{aligned}
 &= \frac{12\sqrt{5}-9\sqrt{2}-16\sqrt{15}+12\sqrt{6}}{62}
 \end{aligned}$$