

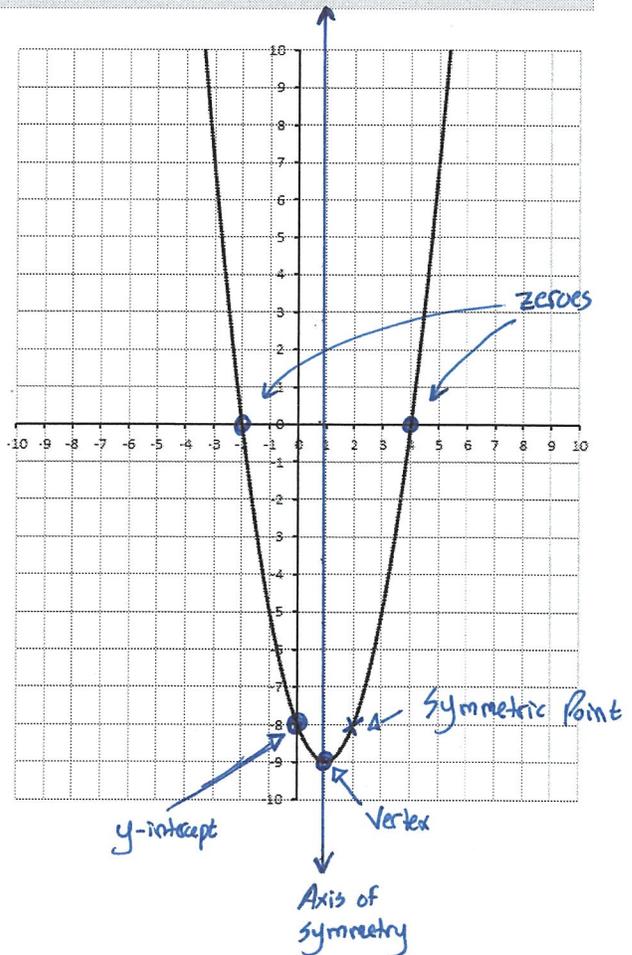
1.11 – Standard Form**Key Ideas**

Definitions:

- Quadratic Function: A function “ f ” whose value $f(x)$ is given by a polynomial of degree two.
- Parabola: The symmetrical curve of the graph of a quadratic function.
- Vertex (of a Parabola): The lowest point of the graph when the graph opens upwards, or the highest point of the graph when the graph opens downwards.
- Minimum value of the function: The lowest value on the Range of a function. For a quadratic function that opens upwards, this would be the y -coordinate of the vertex.
- Maximum value of the function: The greatest value in the range of a function.
- Axis of Symmetry: A line through the vertex that divides the graph of a quadratic function into 2 congruent halves. The x -coordinate of the vertex defines the equation of the axis of symmetry.

Part 1 – Quadratic Functions Introduction

In the quadratic function $f(x) = x^2 - 2x - 8$, what are the important points that you would need if you were to sketch the graph?



Part 2 – Standard Form Transformations

In the equation $(x) = ax^2 + bx + c$, what do adjusting a , b , and c actually do to the graph?

https://phet.colorado.edu/sims/html/graphing-quadratics/latest/graphing-quadratics_en.html

a – Changes shape

b – Moves left/right. Doesn't change shape or y -intercept, so "rocking" motion.

c – y -intercept

Part 3 – Identifying Zeroes, Vertex, y -Intercept, and Axis of Symmetry from a Graph

Zeroes: $x = -5, 1$

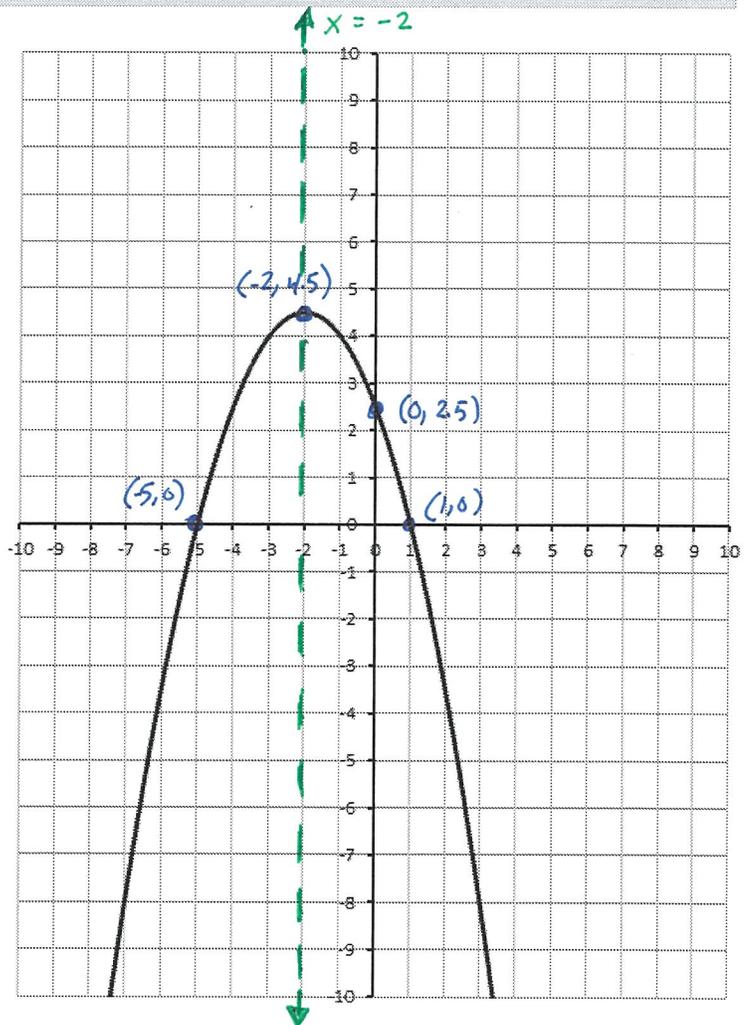
Vertex: $(-2, 4.5)$

y -Intercept: $(0, 2.5)$

Axis of Symmetry: $x = -2$

Maximum: 4.5

Occurs at vertex.



Part 4 – Domain and Range of a Quadratic Function

Domain:

$$\{x \mid -\infty < x < \infty, x \in \mathbb{R}\}$$

or

$$\{x \in \mathbb{R}\} \text{ or } (-\infty, \infty)$$

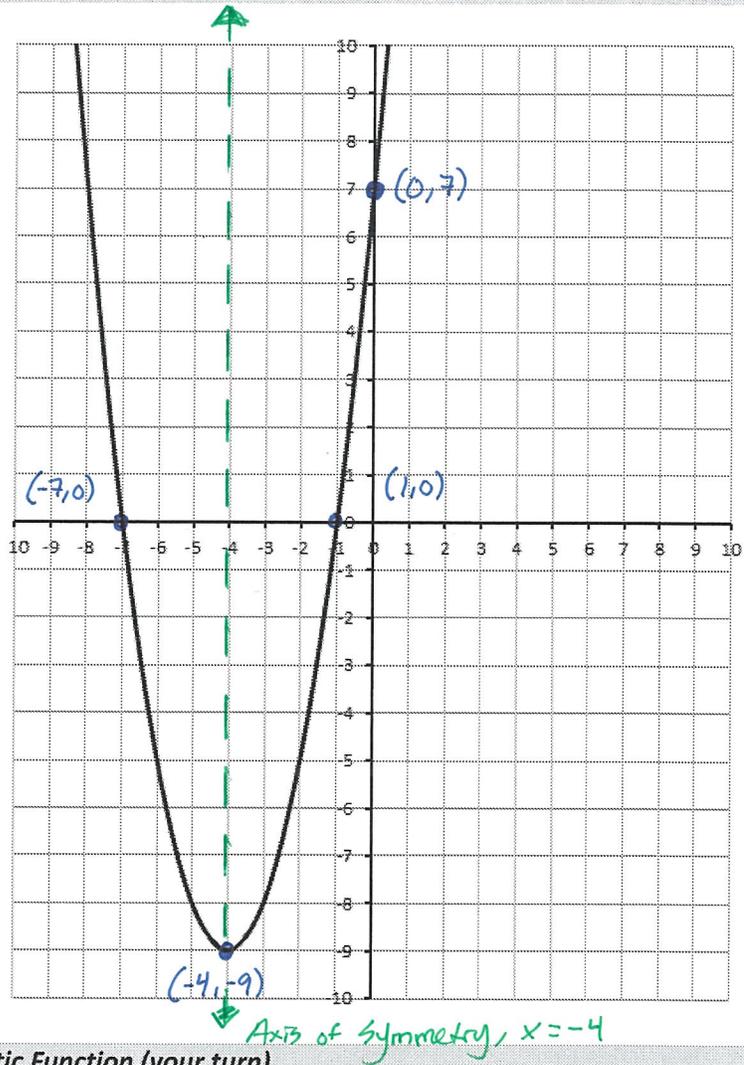
Range:

$$\{y \mid -\infty < y \leq 4.5, y \in \mathbb{R}\}$$

or

$$\{y \mid y \leq 4.5, y \in \mathbb{R}\} \text{ or } (-\infty, 4.5]$$

Part 5 – Identifying Zeroes, Vertex, y-Intercept, and Axis of Symmetry from a Graph (your turn)

Zeroes: $x = -7, 1$ Vertex: $(-4, -9)$ y-Intercept: $(0, 7)$ Axis of Symmetry: $x = -4$ Minimum: -9
Occurs at vertex

Part 6 – Domain and Range of a Quadratic Function (your turn)

Domain:

$$\{x \mid -\infty < x < \infty, x \in \mathbb{R}\}$$

or

$$(-\infty, \infty)$$

Range:

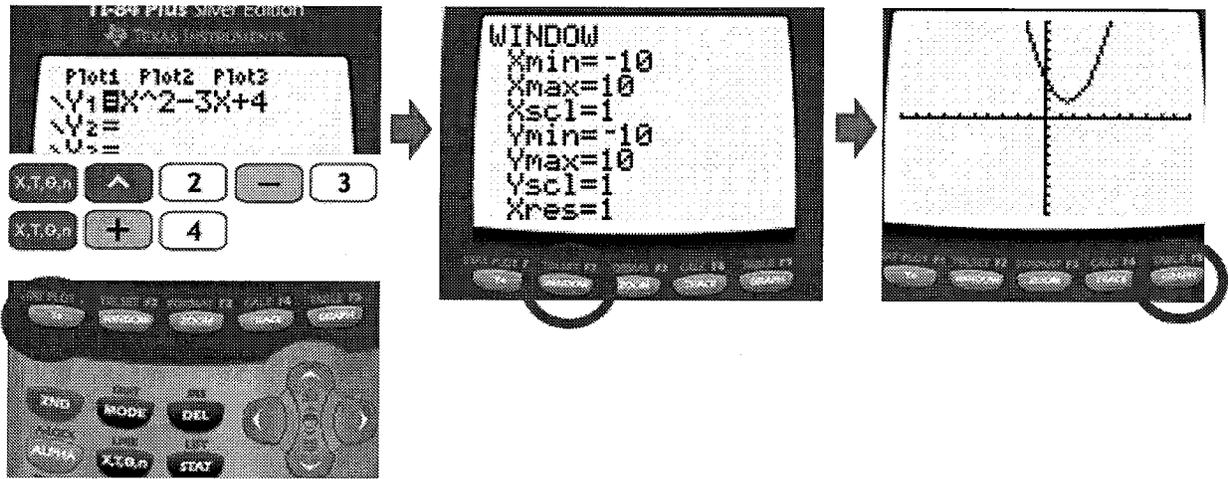
$$\{y \mid -9 \leq y < \infty, y \in \mathbb{R}\}$$

or

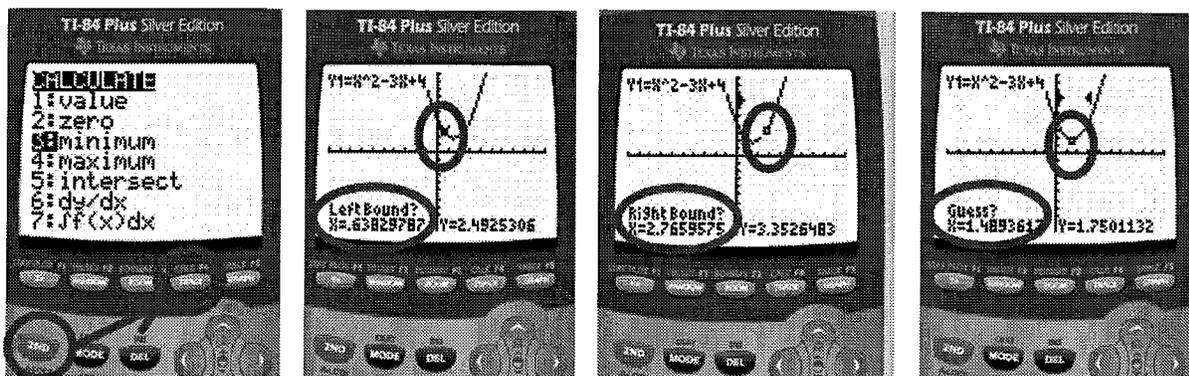
$$[-9, \infty)$$

Part 7 – Using a T.I. Calculator to find Vertex and Zeroes

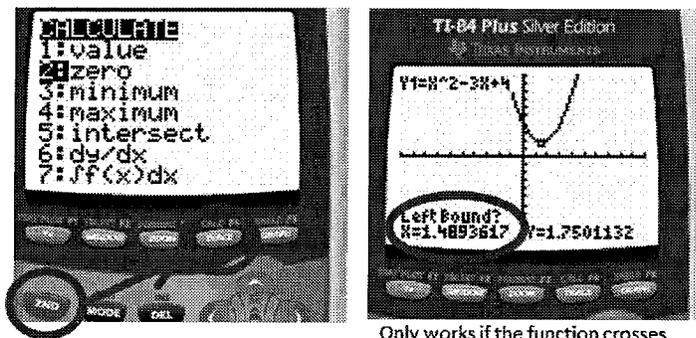
1. With your calculator, graph $f(x) = x^2 - 3x + 4$



2. Find the Max/Min/Vertex



3. Find the Zeroes

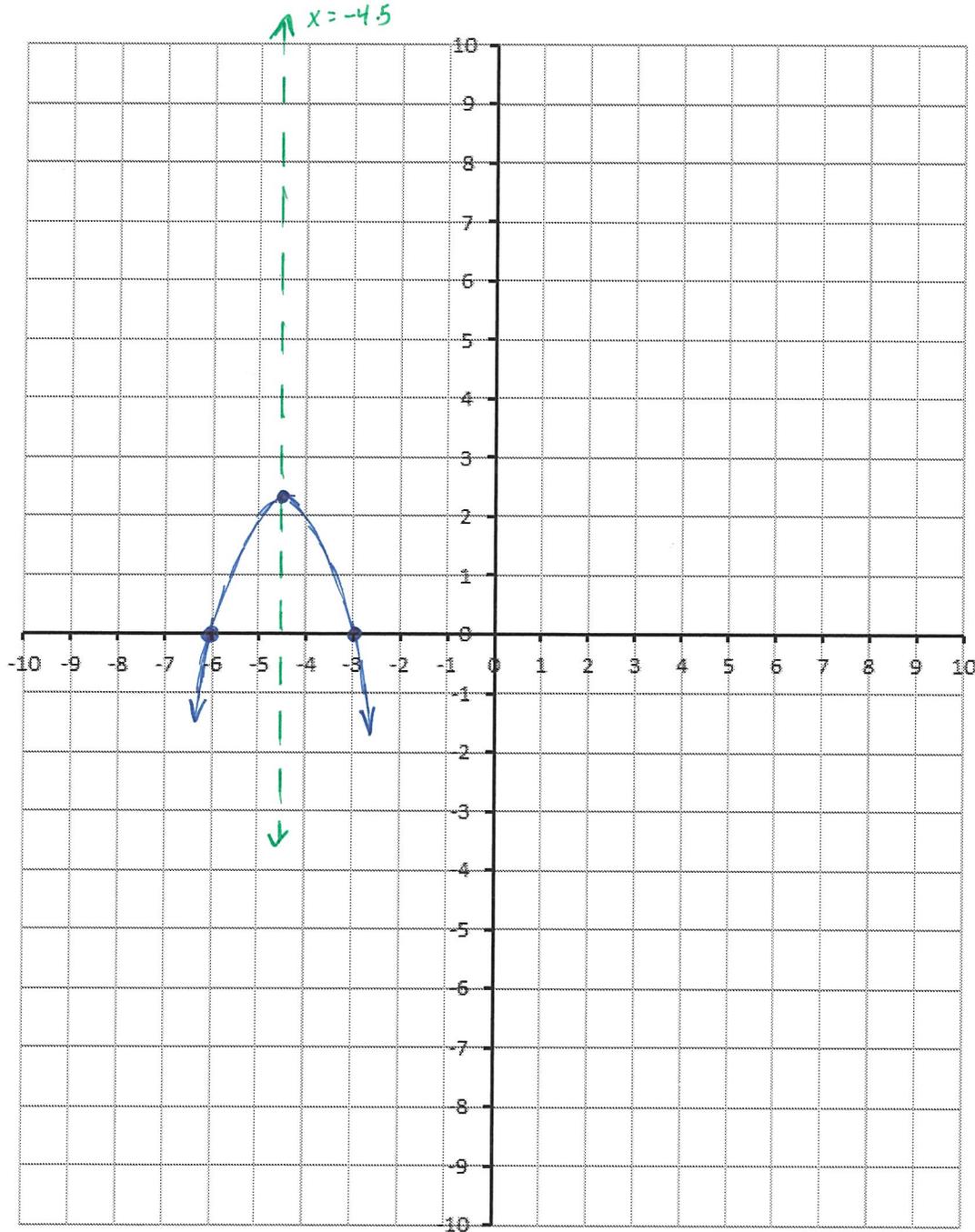


Only works if the function crosses the x-axis (i.e. there is a "zero" value of v)

Using your T.I. Calculator, and given the function $f(x) = -x^2 - 9x - 18$, find

- The Vertex $(-4.5, 2.25)$
- The Maximum value of $f(x)$ 2.25 (Occurs at Vertex)
- The Zeroes $x = -6, -3$
- The equation for the Axis of Symmetry $x = -4.5$

Sketch a quick graph below using these values.



Part 8 – Using Factoring to Find Zeroes

In the quadratic function $f(x) = x^2 - 2x - 8$, for what value of y are the “zeroes” found? Can we determine these values algebraically using factoring?

$$y = x^2 - 2x - 8 \quad \text{x-int when } y = 0$$

$$0 = x^2 - 2x - 8$$

$$0 = (x+2)(x-4)$$

$$x+2=0 \quad x-4=0$$

$$-2 \quad -2 \quad +4 \quad +4$$

$$x = -2 \quad x = 4$$

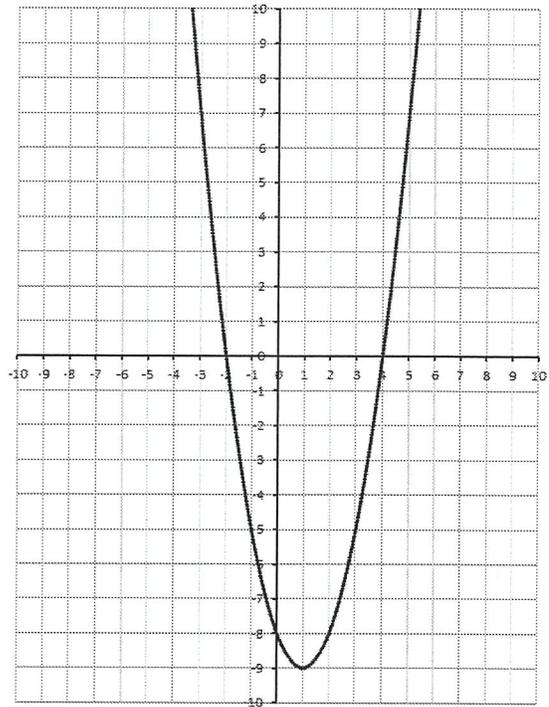
Zeroes at $x = -2, 4$

What is the equation for the axis of symmetry?

Average distance between -2 and 4

$$\frac{(-2) + (4)}{2} = 1$$

$$\boxed{x = 1}$$



In the quadratic function $f(x) = -x^2 - x + 12$, for what value of y are the “zeroes” found? Can we determine these values algebraically using factoring?

$$y = -x^2 - x + 12$$

$$0 = -x^2 - x + 12$$

$$0 = -1(x^2 + x - 12)$$

$$\div(-1) \quad \div(-1)$$

$$0 = x^2 + x - 12$$

$$0 = (x-3)(x+4)$$

$$x-3=0 \quad x+4=0$$

$$+3 \quad +3 \quad -4 \quad -4$$

$$x = 3 \quad x = -4$$

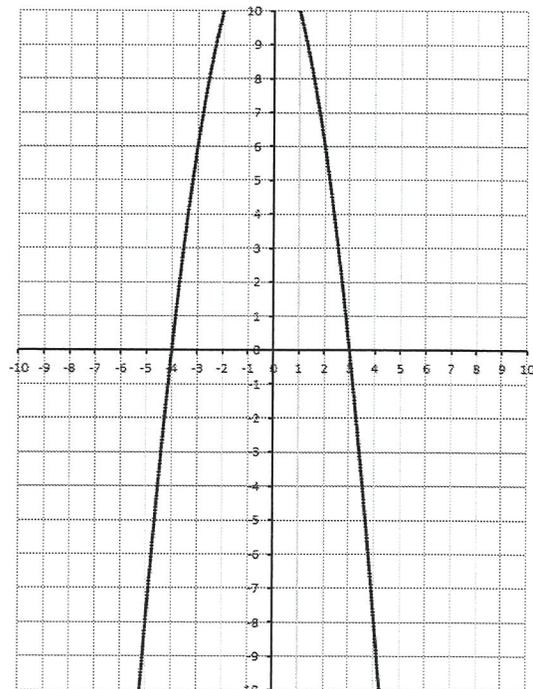
Zeroes at $x = -4, 3$

What is the equation for the axis of symmetry?

Halfway between $-4, 3$

$$\frac{(-4) + (3)}{2} = -0.5$$

$$\boxed{x = -\frac{1}{2}}$$



Part 9 – Putting it all together

Given the equation $f(x) = x^2 - 4x - 5$,

- a. Use factoring to determine the Zeros.

$$0 = x^2 - 4x - 5 \quad \begin{array}{l} +1 \quad -5 \\ \square + \square = -4 \\ \square \times \square = -5 \end{array}$$

$$0 = (x + 1)(x - 5)$$

$$\begin{array}{l} \swarrow \quad \searrow \\ x + 1 = 0 \quad x - 5 = 0 \\ -1 \quad -1 \quad +5 \quad +5 \\ x = -1 \quad x = 5 \end{array}$$

Zeros at $x = -1, 5$

- b. Use the zeros to determine the axis of symmetry.

$$\frac{(-1) + (5)}{2} = 2$$

$$\text{So } x = 2$$

- c. Use the method of your choice to determine the coordinates of the vertex.

- Option #1: Use your T.I. Calculator
- Option #2: Use the x-coordinate (from the axis of symmetry) to find y.
- Option #3: Use calculus to find the x-value, then solve for the y-value.

Option #1: Calculator

Returns value of
(2, -9).

Option #2: Vertex occurs on
axis of symmetry.

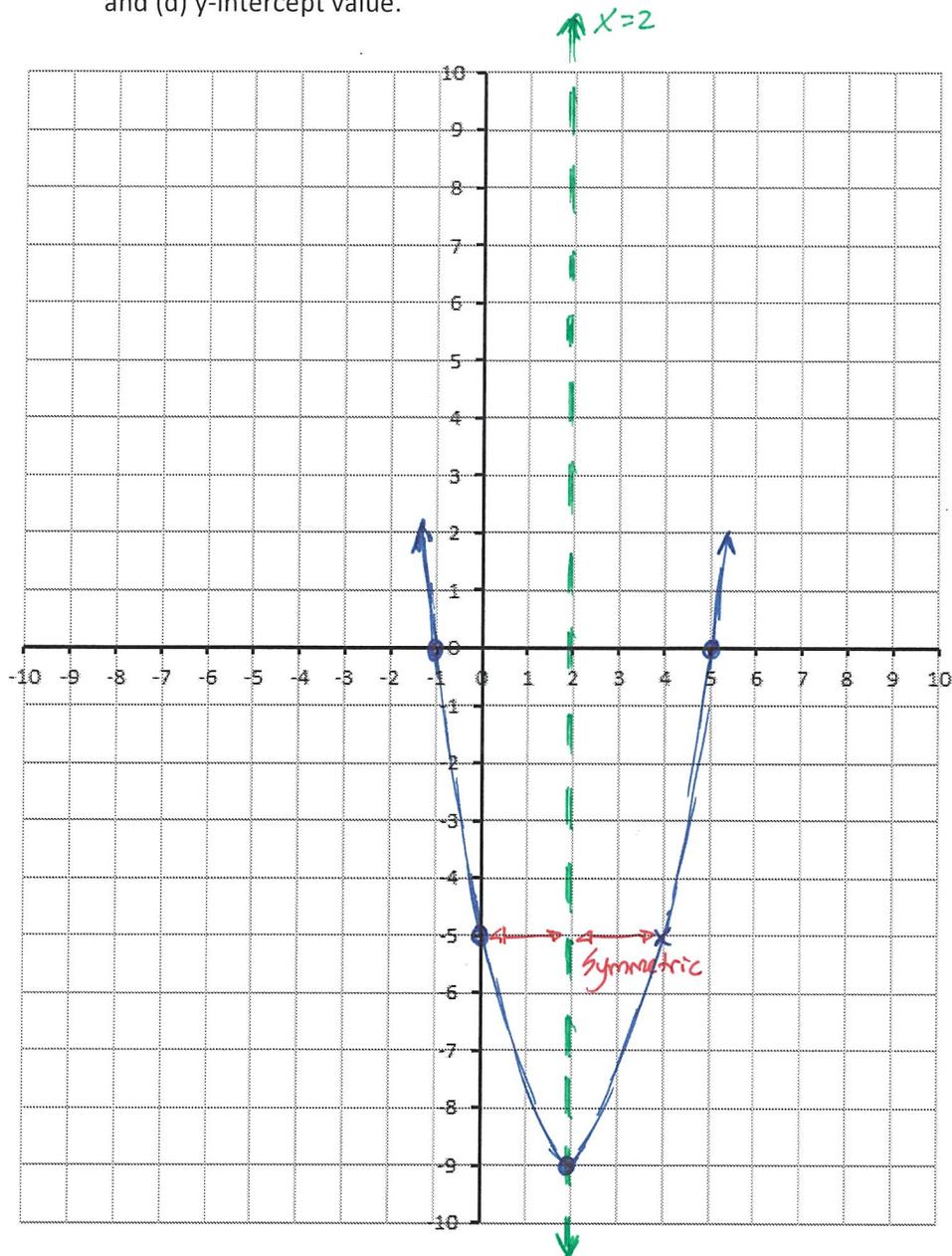
$$\begin{aligned} f(x) &= x^2 - 4x - 5 \\ f(2) &= (2)^2 - 4(2) - 5 \\ &= 4 - 8 - 5 \\ &= -9 \end{aligned}$$

So vertex at (2, -9)

Option #3: Calculus...

This is something I saw
Ma 20-1 students... don't worry
about this for Ma 20-2.

- d. Sketch a graph of the function, with clearly labelled (i) vertex, (ii) zeroes, (iii) axis of symmetry, and (d) y-intercept value.



- e. State the Domain and Range for the function.